



# Transport Properties Electrical Measurements

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# Where Do We Find Tests

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

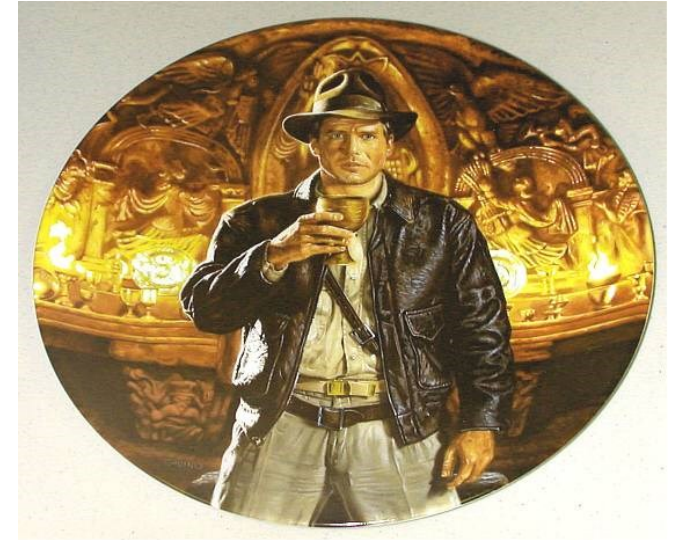
Temperature

Leaching

Acceleration

Field Use

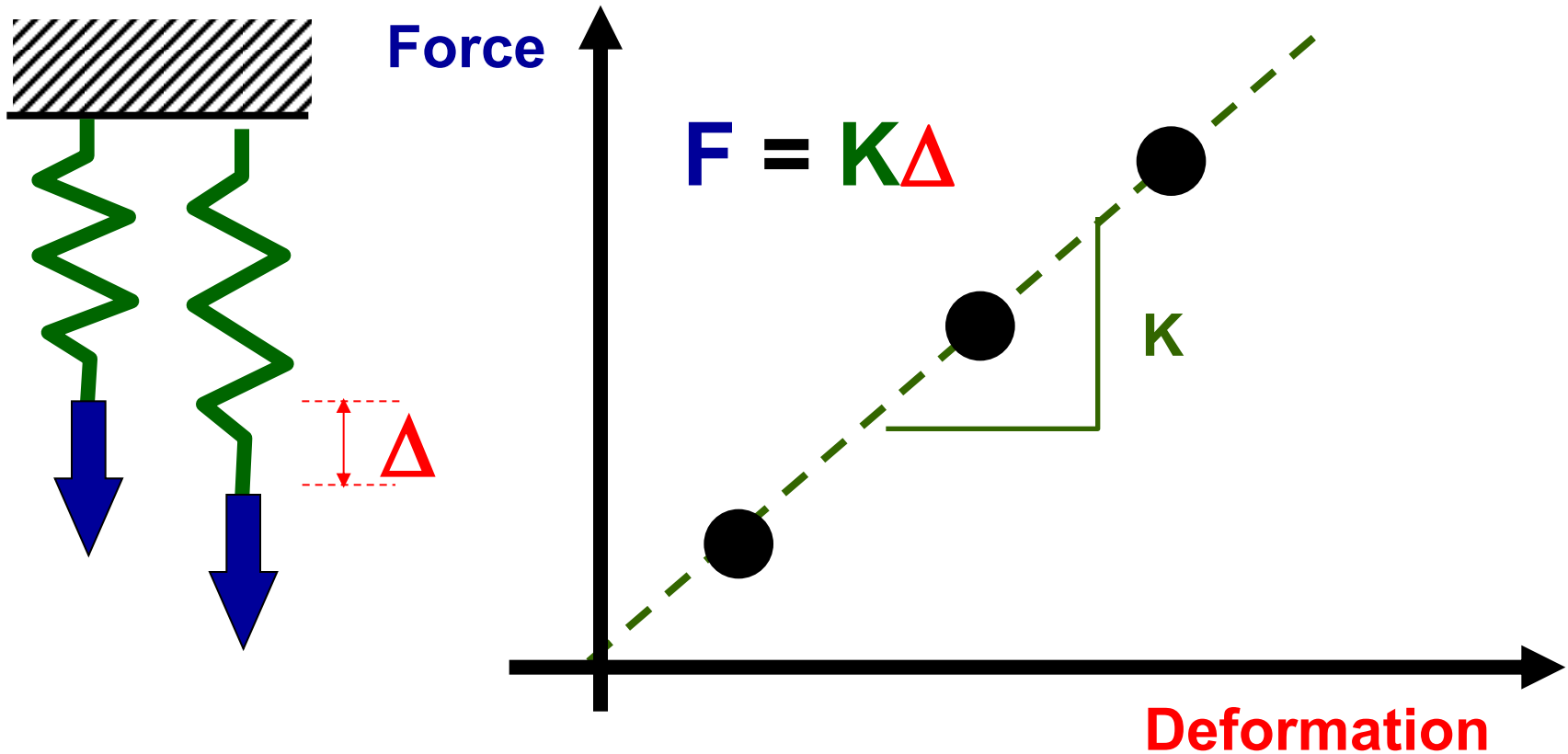
- Much like Indiana we seem to be on the impossible search for the “holy grail”
- We want a test for transport (or durability) that is fast, accurate, inexpensive easy to interpret but it also needs to be scientifically valid
- We think that electrical measurements can be a significant part of this approach





# Recall Many Physical Relations

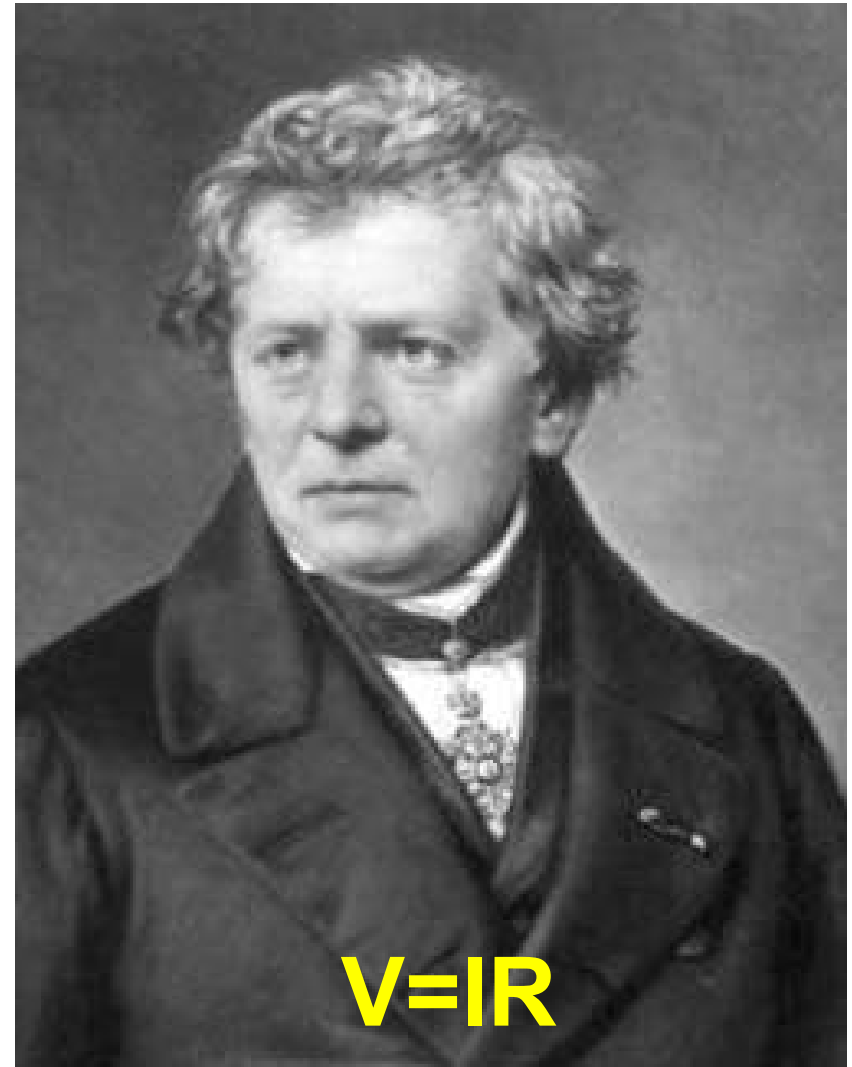
- Recall the relationship between load and deformation





# George Ohm

- German physicist
- Defined fundamental relationships of voltage, current and resistance
- Inspired by Fouriers work on heat conduction
- German Minister of Education proclaimed "a professor who preached such heresies was unworthy to teach science."





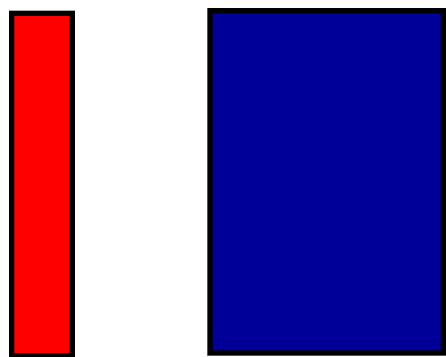
# Henry Cavendish

- British Scientist
- Silent, solitary, shy
- Discovered Hydrogen – Lavoisier ‘named’
- Discovered Ohms Law later identified when Maxwell went through his papers

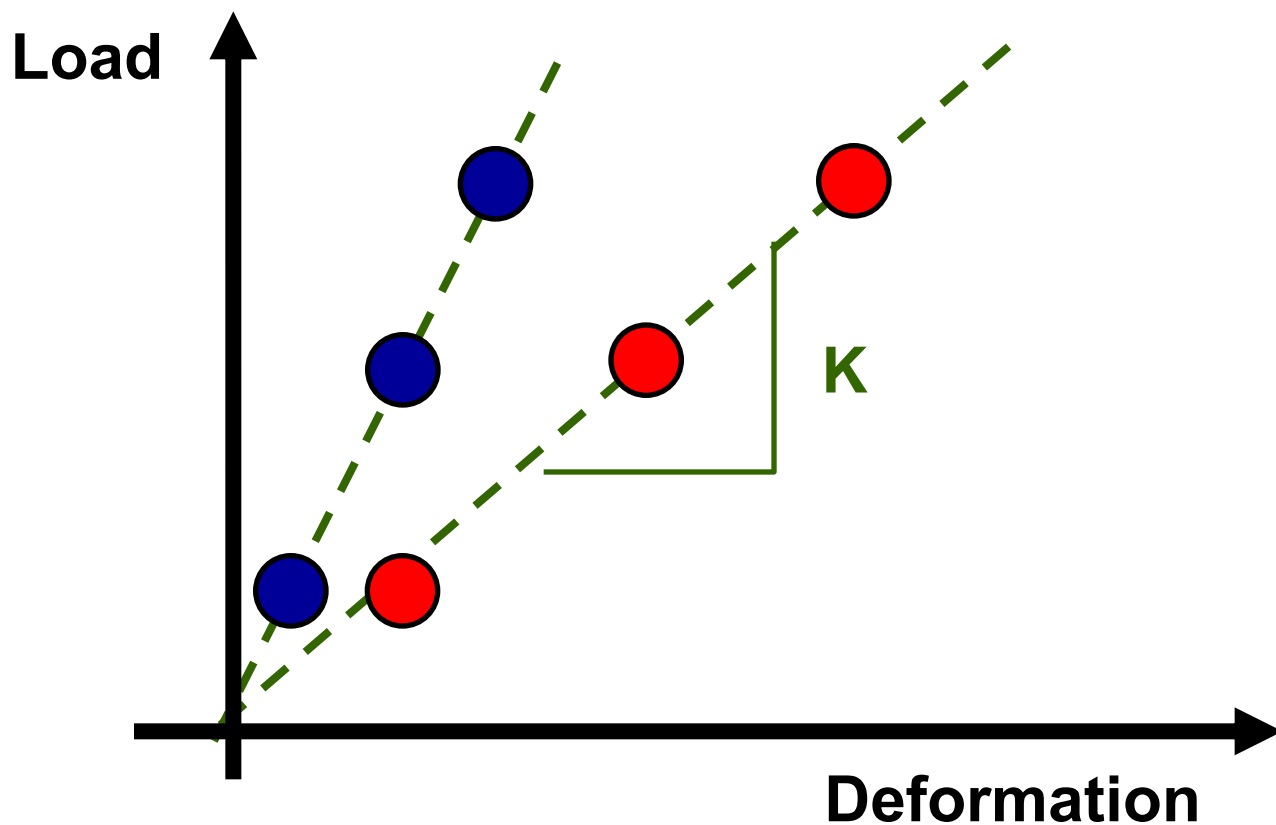




# Does Stiffness Vary Depending on Size



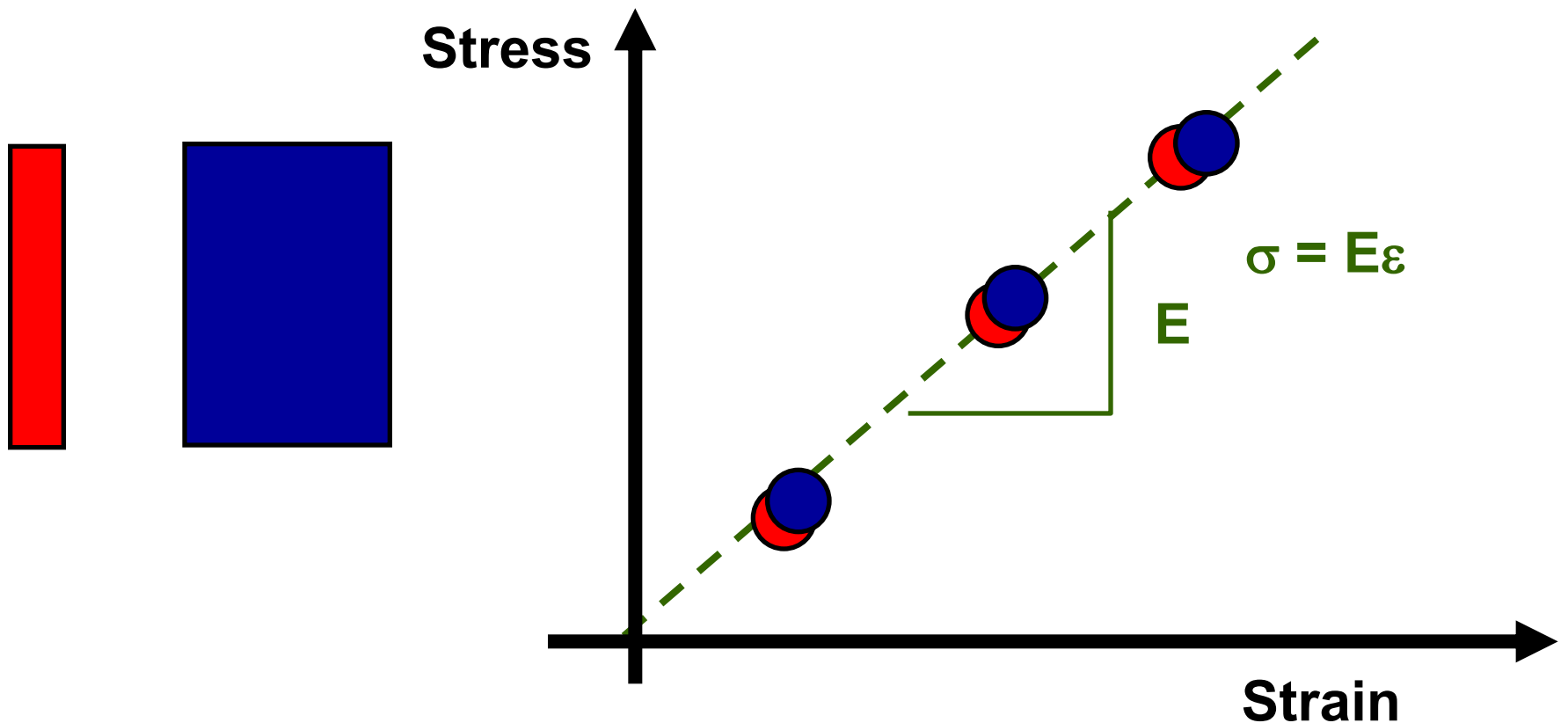
$$F = K\Delta$$





# Instead of Stiffness We Use Elastic Modulus

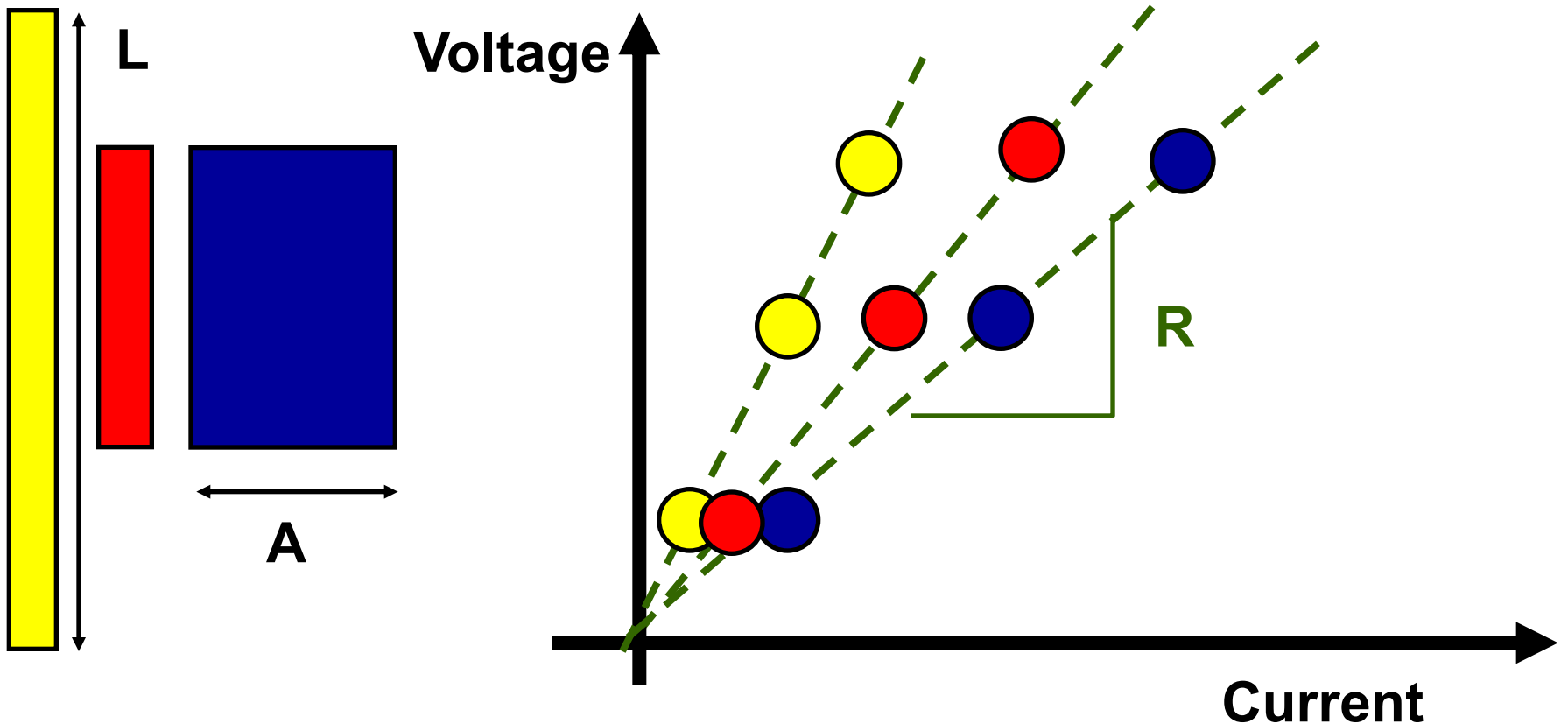
- Is resistance a material property?





# Electrical Resistance

- Is resistance a material property?

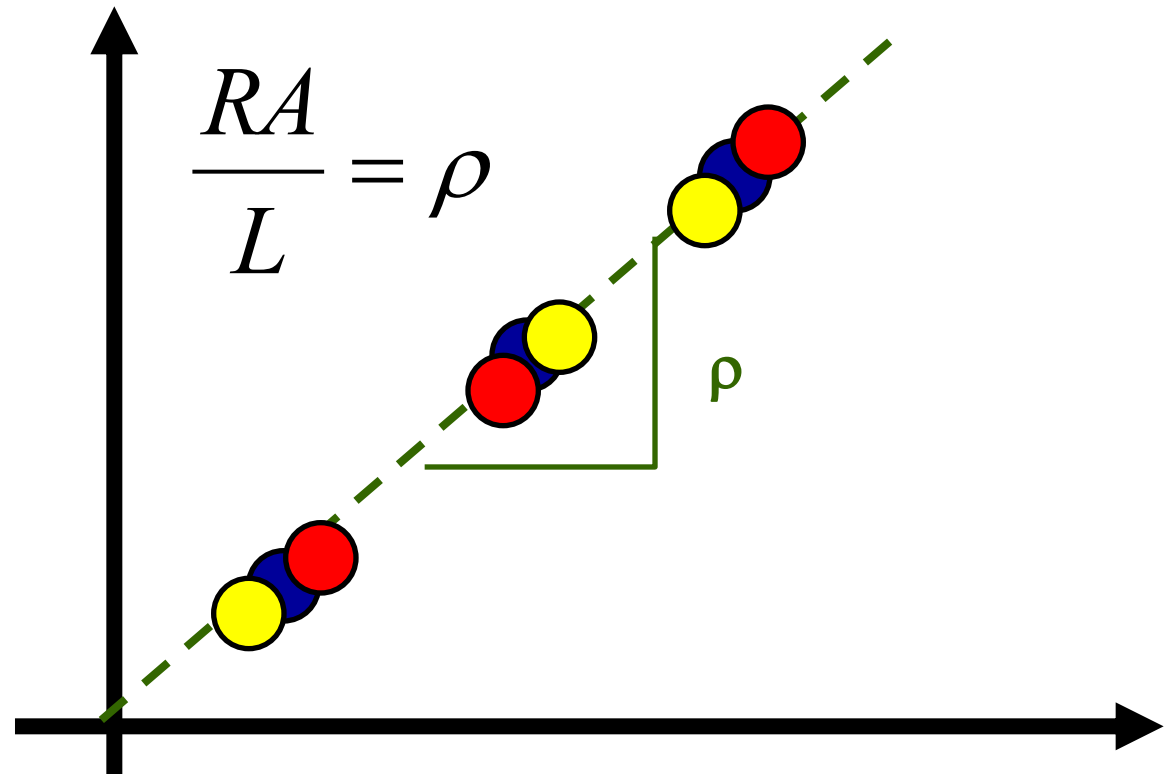
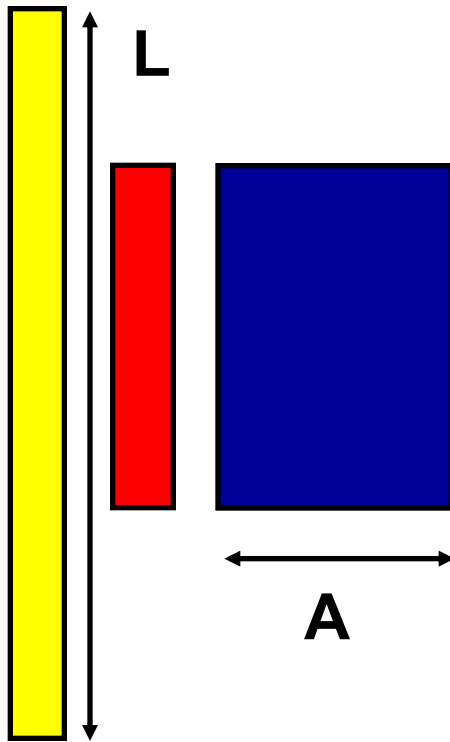






# Electrical Resistance

- Is resistance a material property?





# Conductivity and Other Geometries

$$\sigma = \frac{1}{\rho} = \frac{k}{R}$$

← Geometry Factor (1/m)

← Resistance ( $\Omega$ )

← Resistivity ( $\Omega\text{m}$ )

Conductivity (S/m)

Interchangeable, I find  $\sigma$  easier to think about, however practice seems to like  $\rho$ , so be it



# Rapid Test Methods

$\sigma, \rho$

Geometry

3 Factors

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Tortuosity

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Saturation

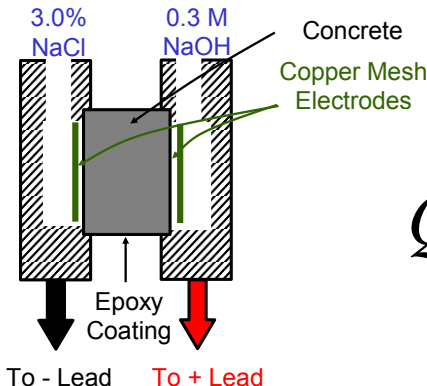
Temperature

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Acceleration

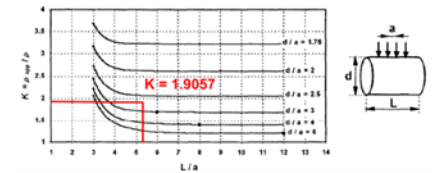
Field Use

- Uniaxial, surface, embedded, and RCPT electrical measurements all yield results that can be directly compared if done properly
- Proper reporting is essential



$$\rho = \frac{V}{I} \frac{A}{L} = \frac{RA}{L}$$

$$\rho = \frac{V}{I} \cdot 2\pi a \cdot \kappa$$

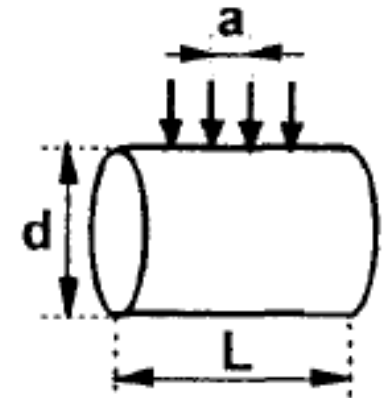
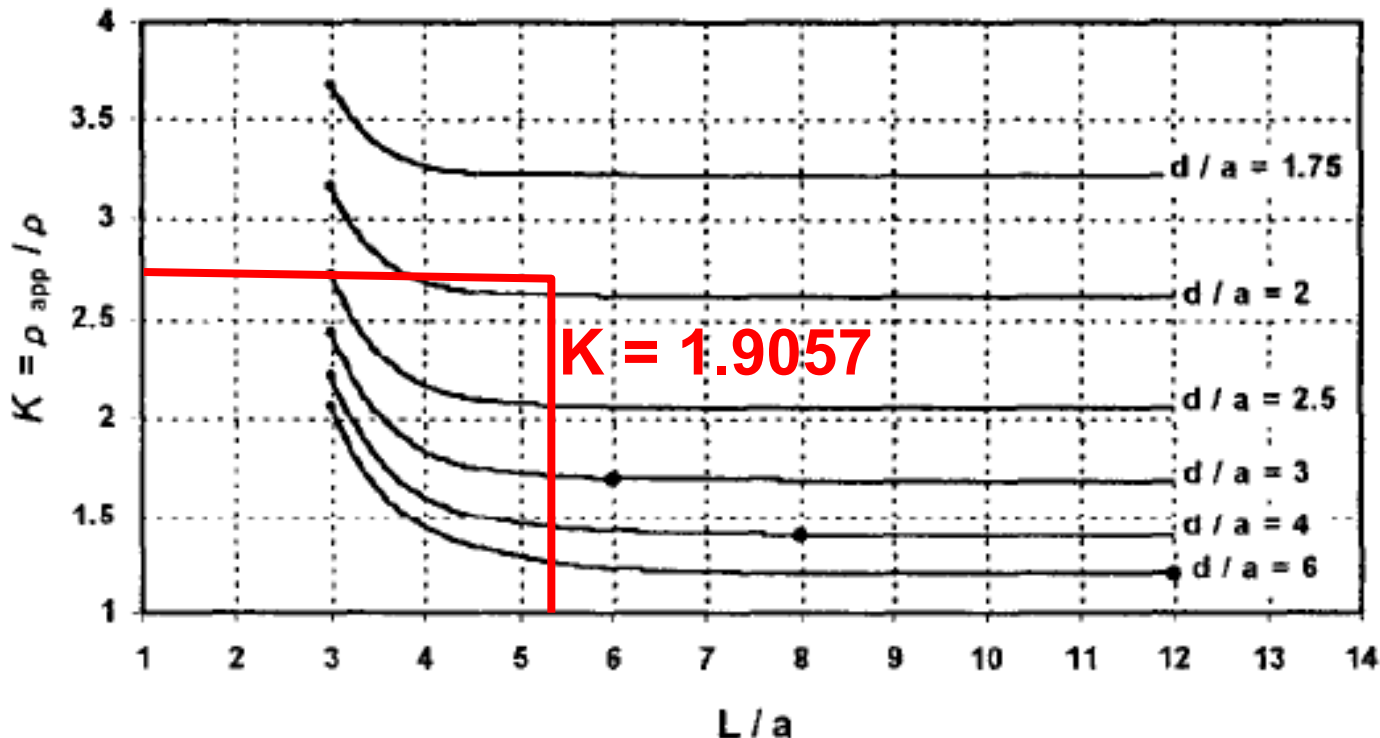


$$Q = \int_{0h}^{6h} \frac{V}{\rho K} dt$$



# Geometry Factor

- Recall the need for a geometry factor
- 4 x 8 cylinder;  $a = 1.5$  in
- $L/a = 8/1.5 = 5.26$        $d/a = 4/1.5 = 2.63$





# RCPT Analyzed

- Coloumb = Amp – Sec
- $I = \text{Coloumb} / (6 \text{ hr} * 60 \text{ min/hr} * 60 \text{ sec/min})$

- $V = 60 \text{ V}$

- $V = I R$

- $R = V / I$

$$Q = \int_{0h}^{6h} \frac{V}{\rho K} dt$$

RCPT	Current	Voltage	Resistance
Coulombs	Amps	V	K-Ohms
6000	0.278	60	0.22
5000	0.231	60	0.26
4000	0.185	60	0.32
3000	0.139	60	0.43
2000	0.093	60	0.65
1000	0.046	60	1.30
500	0.023	60	2.59
100	0.005	60	12.96



# Relationship Between Q (Coloumbs) and Resistivity ( $\rho$ )

$\sigma, \rho$

Geometry

3 Factors

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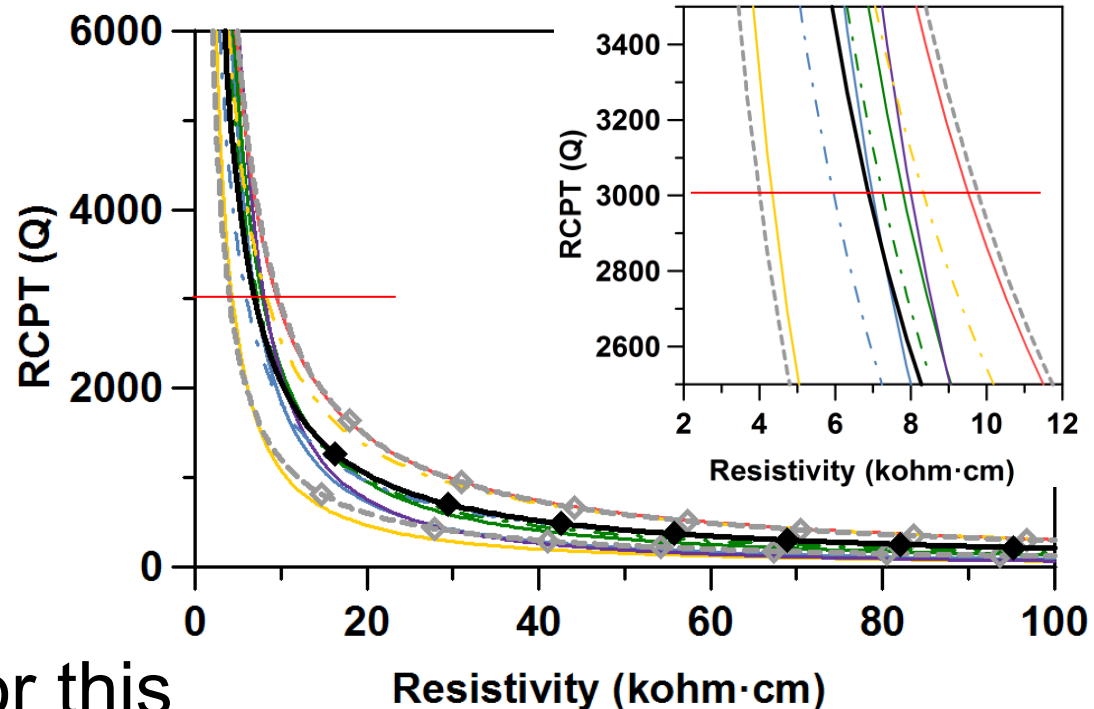
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Field Use

- Many relationships have been developed over the years (the black - theory)  $Q = \int_{0h}^{6h} \frac{V}{\rho K} dt$
- While all have a reasonable shape, details

are very important when one tries to use this in spec's

- Explored reasons for this



Spragg et al. 2013



# Mechanism of Electrical Conduction in Concrete

Concrete is a composite:

- Solid phase (unhyd Cement, CSH, CH,...);  $\sigma_{sol} \approx 10^{-9} \text{ S/m}$

(Rajabipour 2006 based on results of Hammond and Robson 1955)

- Liquid phase (pore solution);

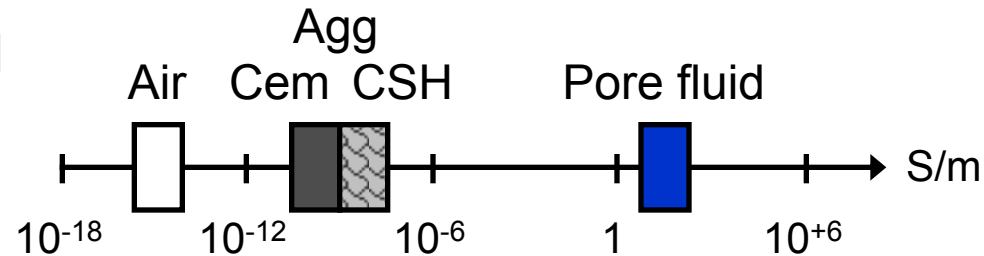
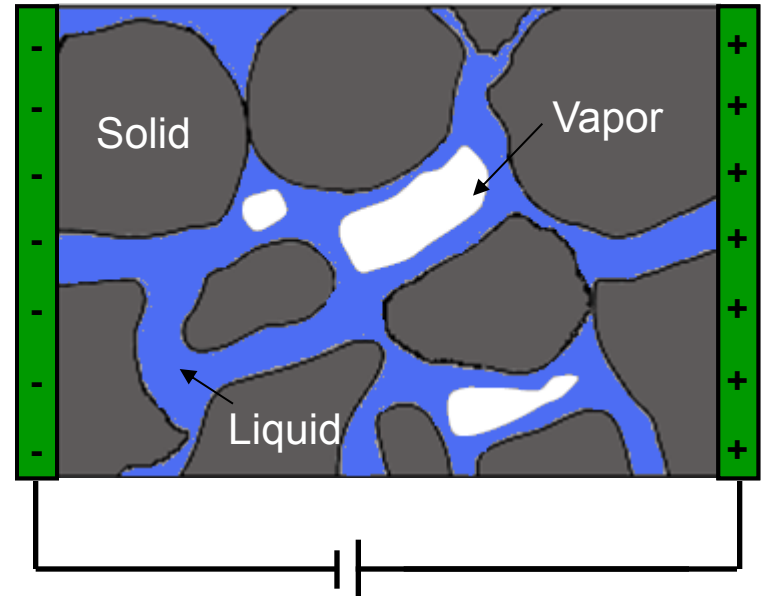
➔  $\sigma_{liq} \approx 1 \text{ S/m to } 20 \text{ S/m}$

(Christensen 1993)

- Vapor phase (air voids, emptied pores);

$\sigma_{vap} \approx 10^{-15} \text{ S/m}$

(Aplin 2005)



Flow of electricity is essentially ionic and through material's liquid phase



# Modified Parallel Law to Model Concrete Conductivity

- Considers pore fluid as the only conductive phase in concrete
- Pore fluid can be in capillary or gel pores or in aggregate pores

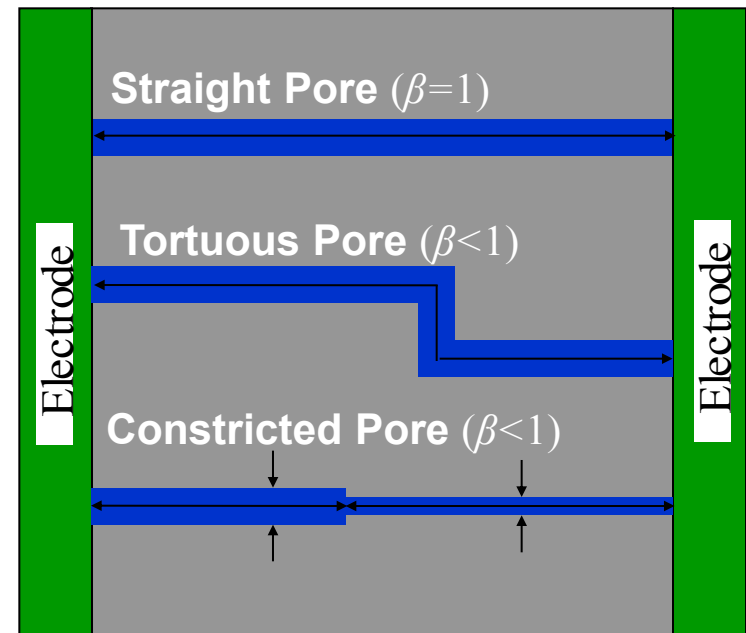
$$\sigma_t = \sigma_o \phi \beta$$

$\sigma_t$ : concrete conductivity (S/m)

$\sigma_o$ : pore solution conductivity (S/m)

$\phi$ : liquid volume fraction

$\beta$ : avg. liquid connectivity  
(describes liquid tortuosity and constrictedness)



(Garboczi 1990, Christensen et al. 1994, Rajabipour 2006)





# Electrolyte

$\sigma, \rho$

Geometry

3 Factors

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Acceleration

Field Use

- Gatorade
- 90 million in royalties to university of florida
- Helps with dehydration maybe even a hangover
- Imbalance of extracellular and interstitial fluid
- Discovered in 1965





# An Electrolyte

$\sigma, \rho$

Geometry

3 Factors

Pore soln

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Tortuosity

Variability

Saturation

Temperature

Leaching

Acceleration

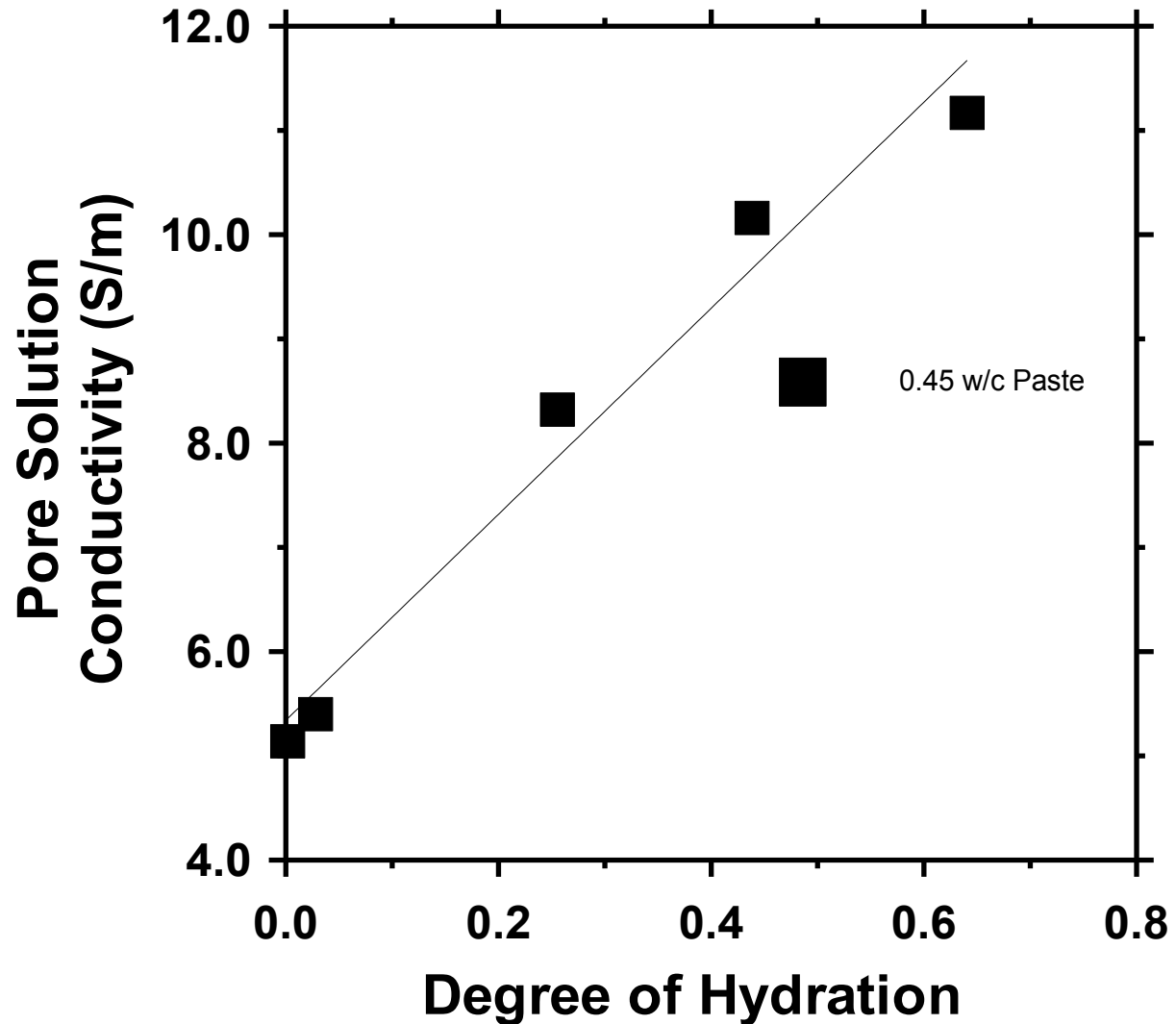
Field Use

- Contains free ions making it electrically conductive (mostly liquids though solids exist)
- Solutions of acids, bases or salts
- Typically form when a salt is placed in a solvent and individual components disassociate due to solvation
- Sodium chloride in water
- Concentrated with high number of ions
- $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Ca}^{2+}$ ,  $\text{Mg}^{2+}$ ,  $\text{Cl}^-$ ,  $\text{HPO}_4^{2-}$ ,  $\text{HCO}_3^-$



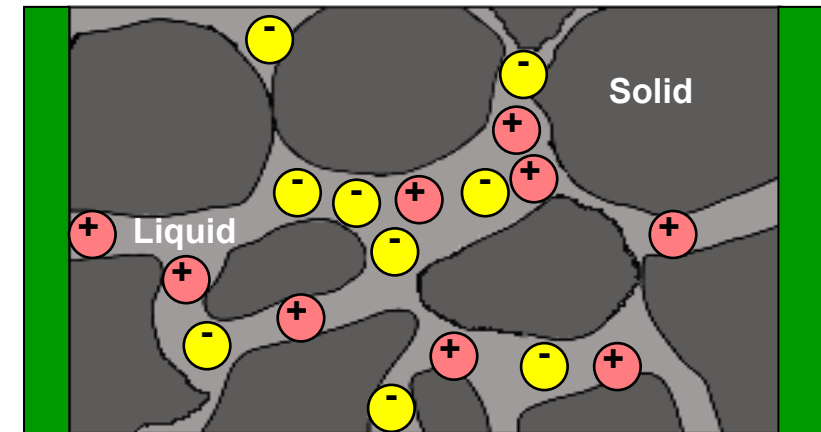
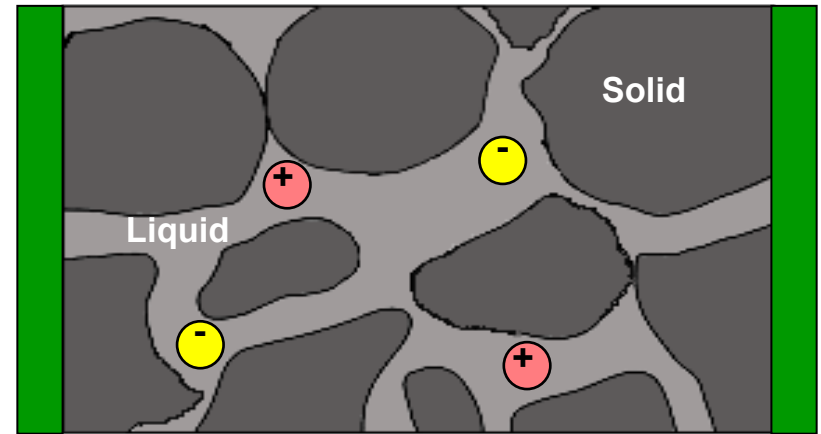
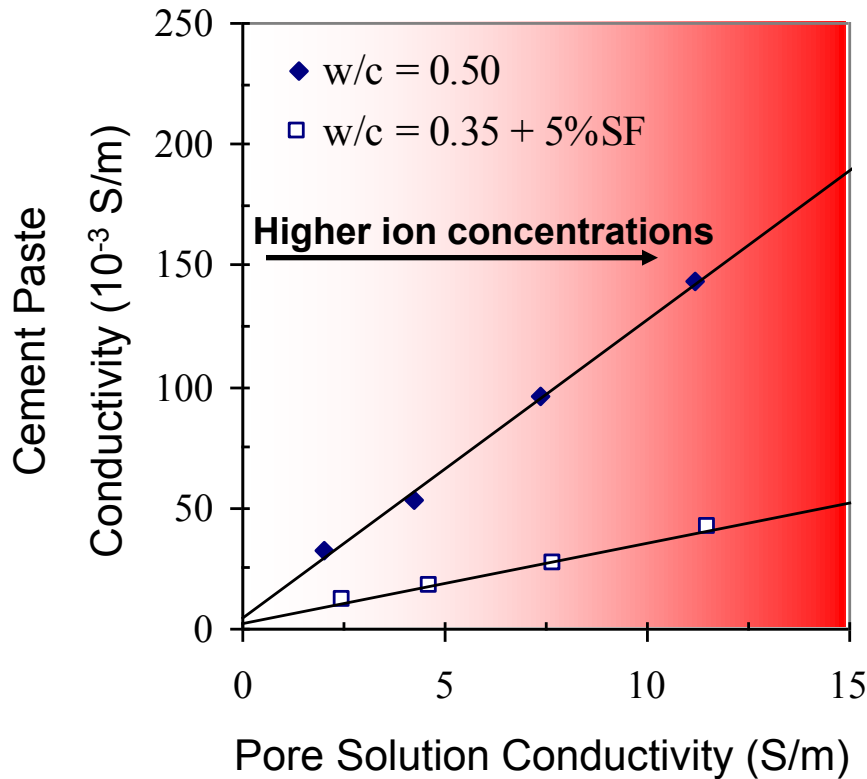
# Pore Solution Conductivity

- Linearly proportional to the DOH
- Pore fluid volume is estimated from Powers or measured with drying





# Pore Fluid Composition



$$\sigma_t = \sigma_o \phi \beta$$

↑                    ↑



# NIST Model

## Estimation of Pore Solution Conductivity

The purpose of this form is to provide an estimate of the electrical conductivity (S/m) of the pore solution in a concrete based on the mixture proportions and achieved degree of hydration.

It is assumed that 75 % of the sodium and potassium initially present as oxides in the cement-based materials will be released into the pore solution. In the presence of silica fume, more alkalis are absorbed by the products of the pozzolanic reactions and "free" alkali ions are further reduced. This calculation only considers the alkali ions and their accompanying hydroxides and not others such as chlorides, etc.

### Mixture Proportions

Material	Mass (kg or lb)	Na <sub>2</sub> O content (mass %)	K <sub>2</sub> O content (mass %)	SiO <sub>2</sub> content (mass %)
Water	160.0	Not applicable	Not applicable	Not applicable
Cement	400.0	0.2	1.0	Not applicable
Silica fume	20.0	0.2	0.2	99.0
Fly ash	0.0	0.2	0.2	50.0
Slag	0.0	0.2	0.5	Not applicable

Estimated system degree of hydration (%): 70

Hydrodynamic viscosity of pore solution relative to water: 1.0

Curing: Saturated  Sealed

Estimated pore solution composition (M):

K<sup>+</sup>: 0.0

Na<sup>+</sup>: 0.0

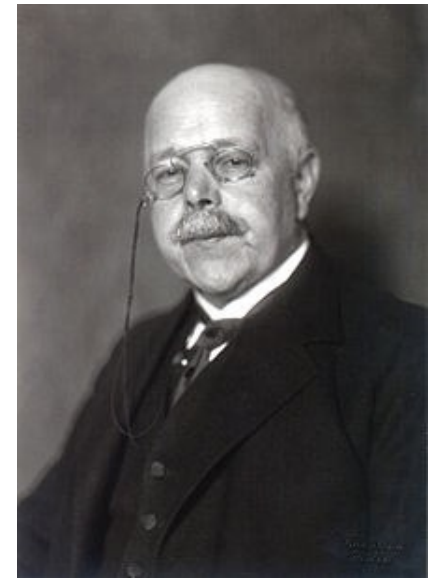
OH<sup>-</sup>: 0.0

<http://ciks.cbt.nist.gov/poresolncalc.html>



# Walther Nernst

- Walther Hermann Nernst (1864-1941)
- a German physical chemist and physicist who is known for his theories behind the calculation of chemical affinity
- he won the 1920 Nobel Prize
- establish field of physical chemistry and contributed to electrochemistry, thermodynamics
- known for developing the Nernst equation.





# From Resistivity to Diffusivity

## Nernst Einstein Relationship

$\sigma, \rho$

Geometry

3 Factors

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Acceleration

Field Use

- Walther Nernst  $\frac{\sigma_t}{\sigma_o} = \frac{D_i}{D_i^\mu}$   
(1864-1941)
- German physical chemist/physicist
- Won 1920 Nobel Prize

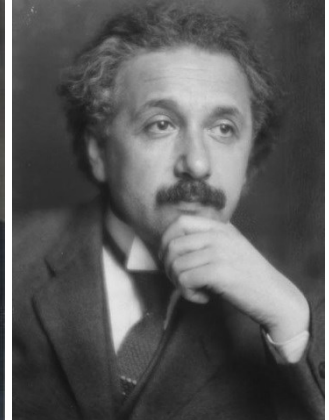
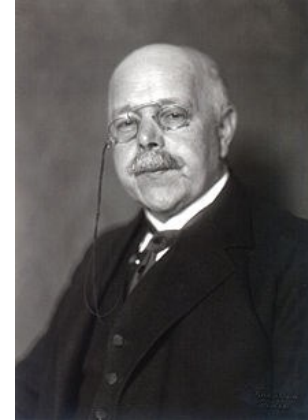


Table 1 – Diffusion coefficient of various species in free water

Species	$D_i^\mu$ ( $10^{-9} \text{ m}^2/\text{s}$ )
OH <sup>-</sup>	5.273
Na <sup>+</sup>	1.334
K <sup>+</sup>	1.957
SO <sub>4</sub> <sup>2-</sup>	1.065
Ca <sup>2+</sup>	0.792
Cl <sup>-</sup>	2.032
Mg <sup>2+</sup>	0.706

$$\frac{\rho_{Pore}}{\rho_{Bulk}} = \frac{D_i}{D_i^\mu} = \frac{1}{F}$$

$$D_i = D_i^\mu \cdot \frac{\rho_{Pore}}{\rho_{Bulk}}$$

$$D_i = D_i^\mu \cdot \phi\beta = D_i^\mu \cdot \frac{1}{F}$$



# Simple Composite Models

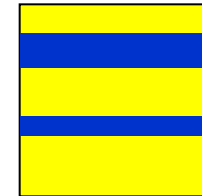
NAME

FORMULA

MICROSTRUCTURE

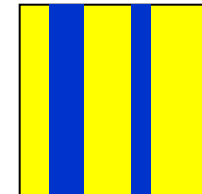
Parallel

$$D_{bulk} = D_1\phi_1 + D_2\phi_2$$



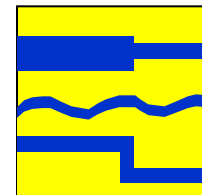
Series

$$1/D_{bulk} = (\phi_1/D_1) + (\phi_2/D_2)$$



Modified  
Parallel

$$D_{bulk} = D_1\phi_1\beta_1 + D_2\phi_2\beta_2$$

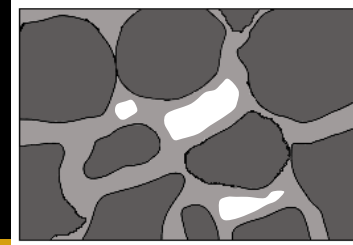






# Composite Conductivity Models

## Single Conductive Phase



**Second group:** consider volume fractions and phase geometries

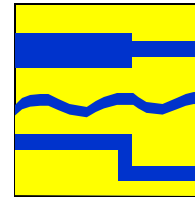
NAME

FORMULA

MICROSTRUCTURE

Modified Parallel

$$\sigma_t = \sigma_o \phi_o \beta_o$$



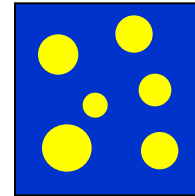
Archie's

$$\sigma_t = \sigma_o \phi_o^{m_o}$$

Sedimentary Rocks

Maxwell

$$\sigma_t = \sigma_o \left[ \frac{(d-1)\phi_o}{d-\phi_o} \right]$$

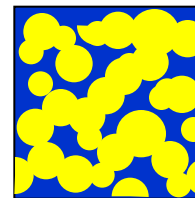


DEM

$$\sigma_t = \sigma_o \phi_o^{(d/(d-1))}$$

Self-Consistent (SC)

$$\sigma_t = \sigma_o \left[ \frac{d\phi_o - 1}{d - 1} \right]$$



- $d$  describes spatial dimension not phase geometries
- But, it has been used empirically to describe phase geometries

(McLachlan et al. 1990, Torquato 2002)



# Parallel Law Modified

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

Temperature

Leaching

Acceleration

Field Use

- Considers pore fluid as the only conductive phase
- Pore fluid (capillary, gel pores)

$$\rho_{Bulk} = \rho_{Pore} \cdot \frac{1}{\phi\beta} = \rho_{Pore} \cdot F$$

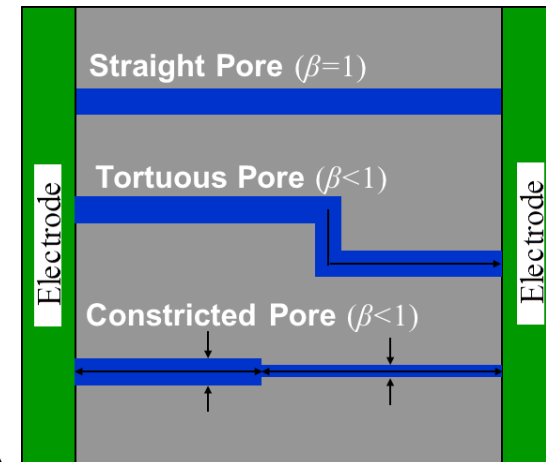
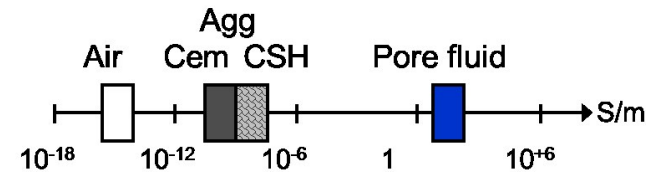
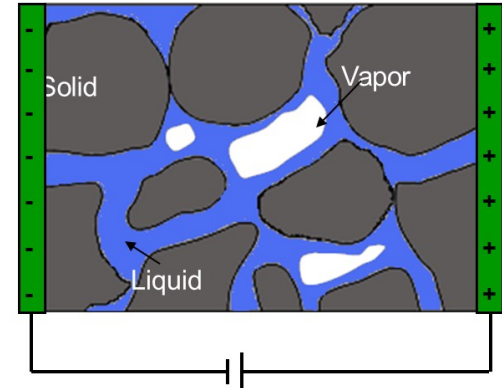
$\rho_{Bulk}$ : concrete conductivity (S/m)

$\rho_{Pore}$ : pore solution conductivity (S/m)

**F**: Formation Factor

$\phi$ : pore volume fraction

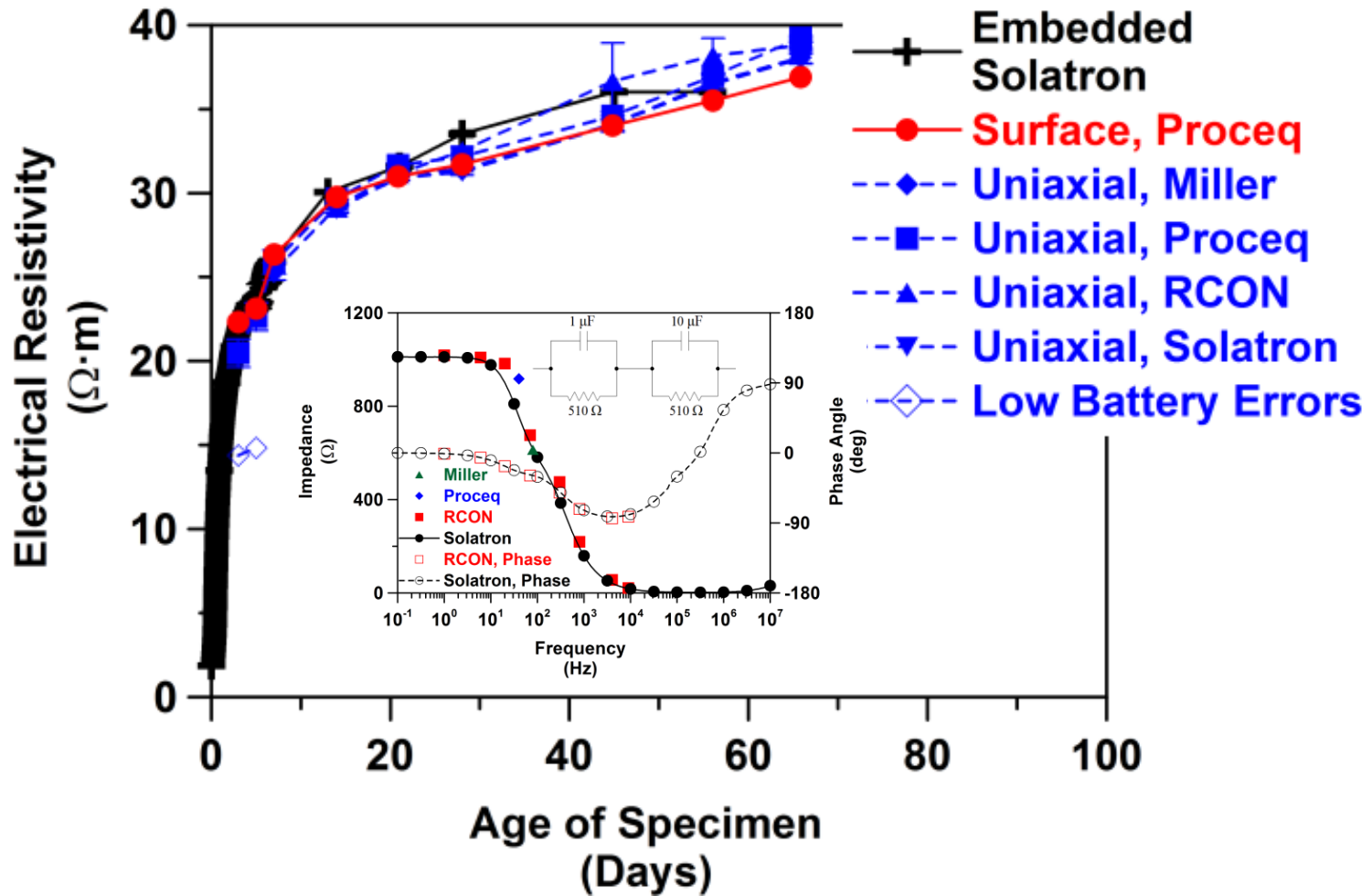
$\beta$ : avg. liquid connectivity (describes liquid tortuosity and constrictedness)  
(Garboczi 1990, Christensen et al. 1994, Rajabipour 2006)





# Comparison of Different Manufacturers

- $\sigma, \rho$
- Geometry
- 3 Factors
- Pore soln
- Porosity
- Tortuosity
- Variability
- Saturation
- Temperature
- Leaching
- Acceleration
- Field Use



Spragg et al. 2012



# Lets Start with Notation and Archie

$\sigma, \rho$

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Acceleration

Field Use

- Using resistivity, while I prefer conductivity, tests in practice that have discussion in  $\rho$

$$\rho = \frac{1}{\sigma}$$

- Assume the only conductive phase is the fluid and the resistivity of the concrete is the product of resistivity of solution and the formation factor (inverse porosity and connectivity) (solutions exist for other conductive phases Weiss et al.)



$$\rho = \rho_0 \frac{1}{\phi} \frac{1}{\beta}$$



# Relationship Between Q (Coloumbs) and Resistivity ( $\rho$ )

$\sigma, \rho$

Geometry

3 Factors

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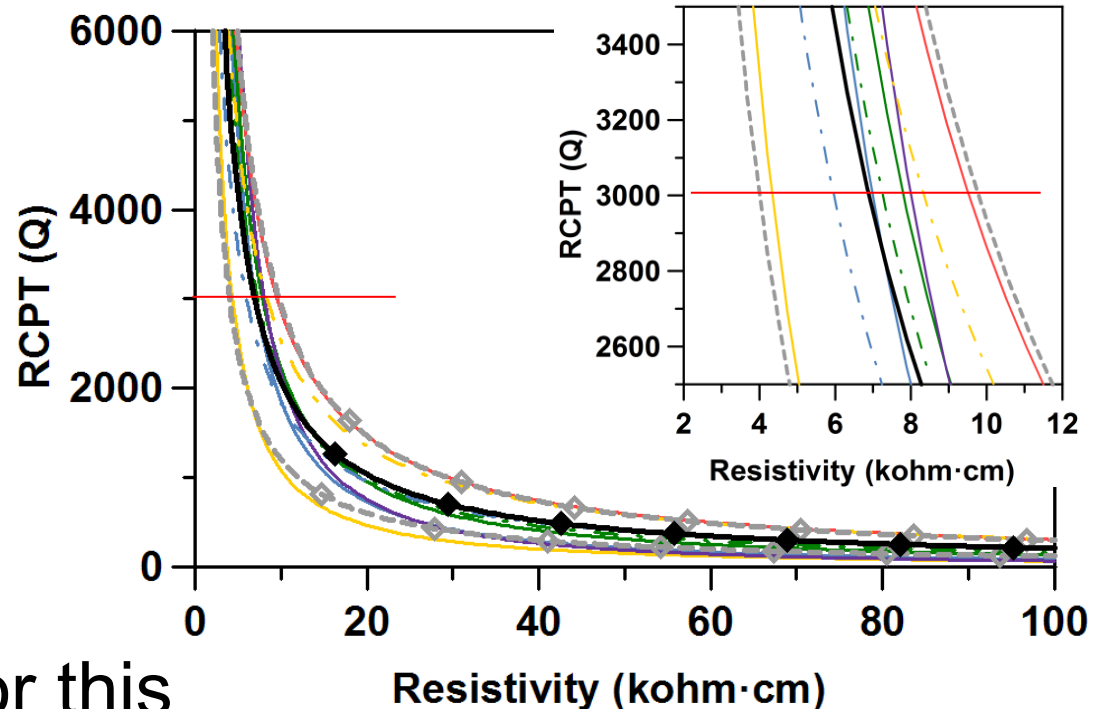
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- Many relationships have been developed over the years (the black - theory)  $Q = \int_{0h}^{6h} \frac{V}{\rho K} dt$
- While all have a reasonable shape, details

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- Explored reasons for this



Spragg et al. 2013



# Components of Variation

$\sigma, \rho$

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Field Use

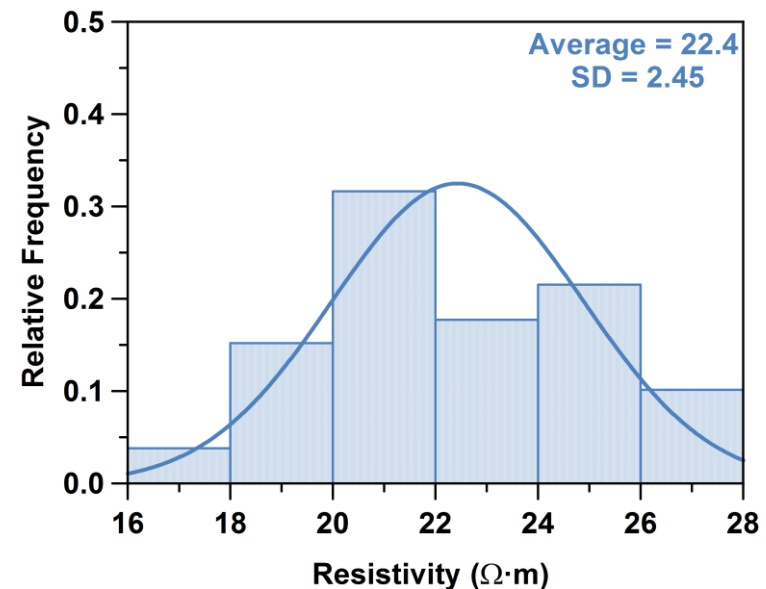
$$\sigma_{total} = \sqrt{\sigma_{machine}^2 + \sigma_{operator}^2 + \sigma_{material}^2 + \sigma_{production}^2 + \sigma_{curing}^2}$$

- Machine/Operator/Material

- Traditionally estimated in a single lab as
- 3-4% (Purdue, LaDOT)

- Production

- Important when used as a QC/QA tool
- Dependent on contractor quality
- 10% is a typical value



- Data shown is from a central mix plant with one mixture run frequently, low variation

Spragg et al. 2012



# Components of Variation Attention to Curing is Critical

$\sigma, \rho$

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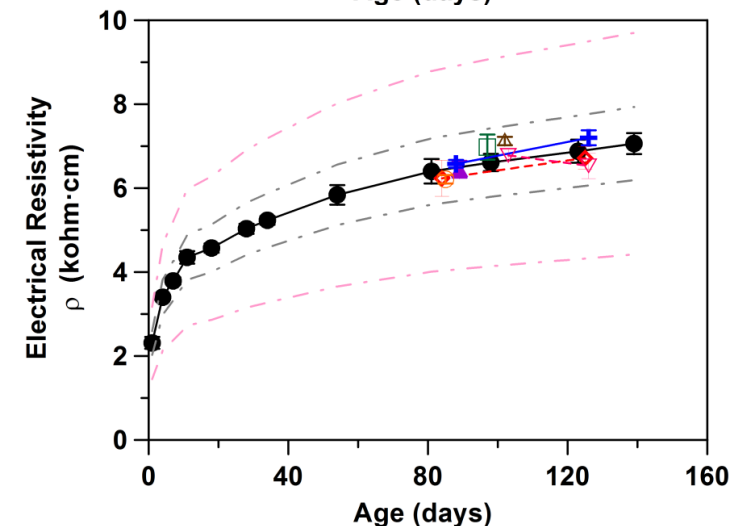
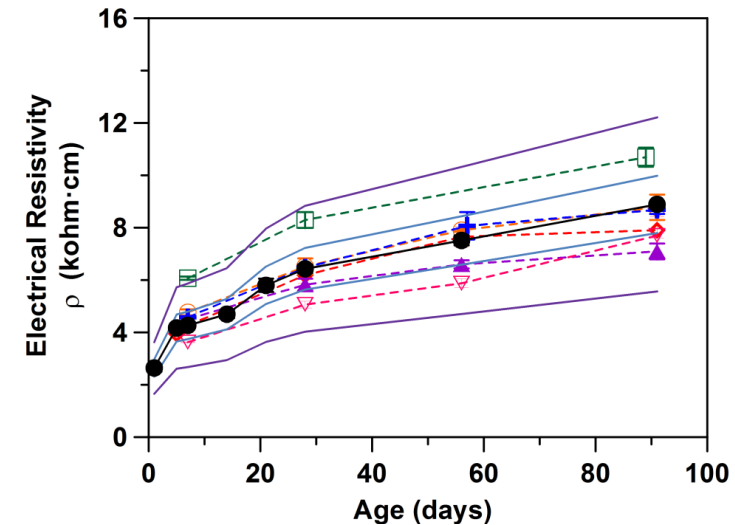
Temperature

Leaching

Acceleration

Field Use

- AASHTO RR (12)
- Within-lab: 4.36%
  - Machine/Operator/ Material
- Multi-lab: 13.22%
  - Machine/Operator/ Material and curing
  - **Believed Curing Variation: 12.5%**
- State Variation Shown (top young, bottom old samples)



Spragg et al. 2013



# Incorporating Aspects of Curing

$\sigma, \rho$

Geometry

3 Factors

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Acceleration

Field Use

- Spragg developed a program to investigate factors that could influence curing (not discussing temp or RH here that change DOH)

$$\rho = \rho_o^* \cdot F \cdot f(S) \cdot f(T_{Testing}) \cdot f(Leach)$$

- $\rho$  is the resistivity at an equivalent age  $t_{equivalent}$
- $\rho_o^*$ : pore solution resistivity at saturation
- $f(S)$  saturation function
- $f(T_{testing})$  testing temperature correction
- $f(Leach)$  leaching function

Spragg et al. 2013





# Degree of Saturation and Its Impact on Transport

$\sigma, \rho$

Geometry

3 Factors

Pore soln

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Tortuosity

Variability

Saturation

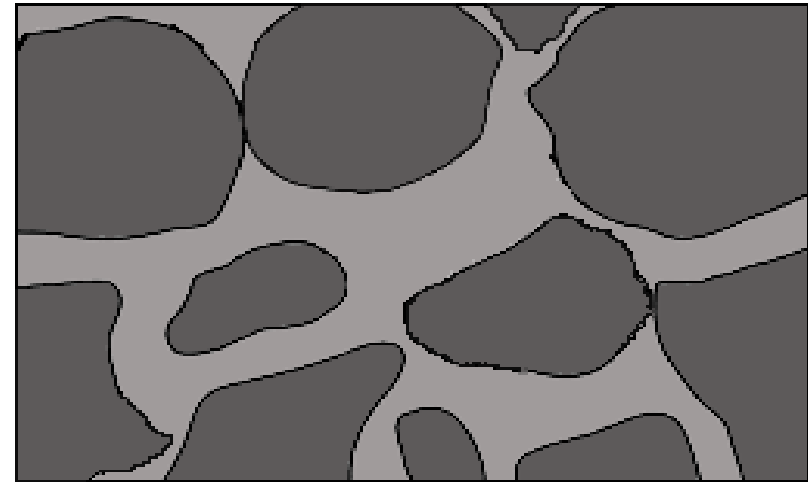
Temperature

Leaching

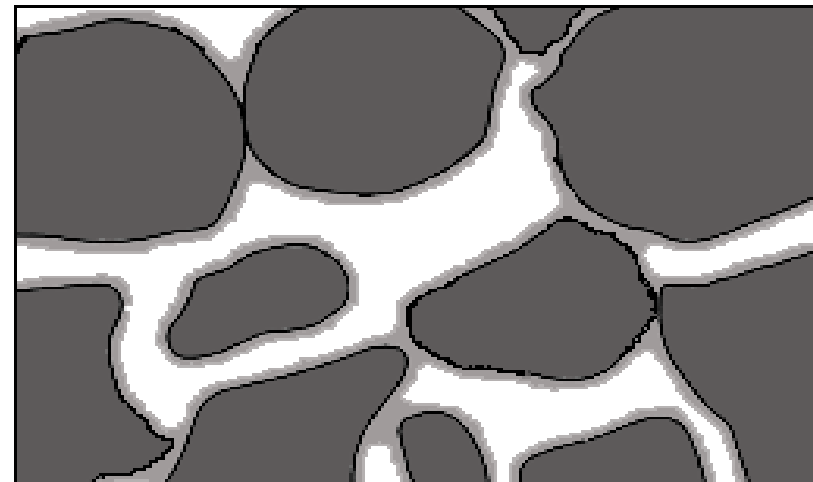
Acceleration

Field Use

- Transport in the fluid phase depends on the volume and connectivity of the fluid phase
- Transport in the vapor phase depends on the volume and connectivity of the vapor phase



Saturated

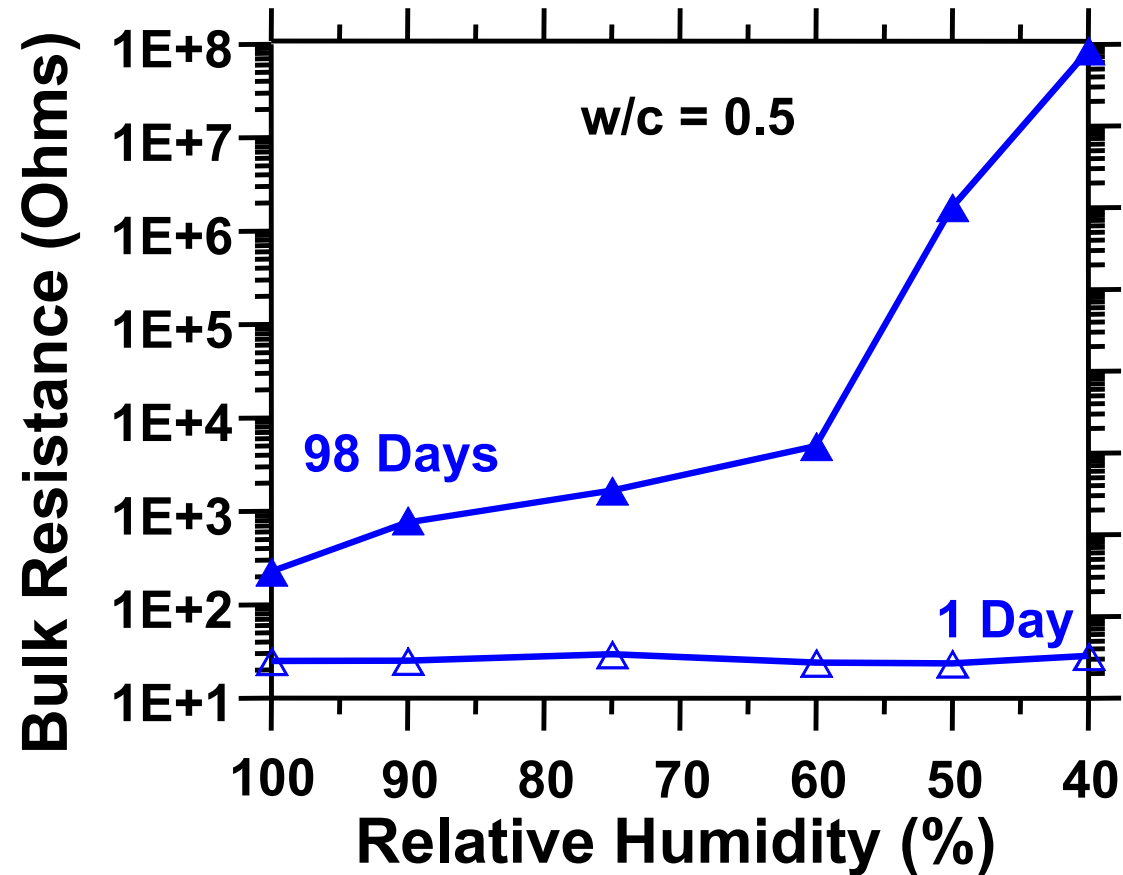
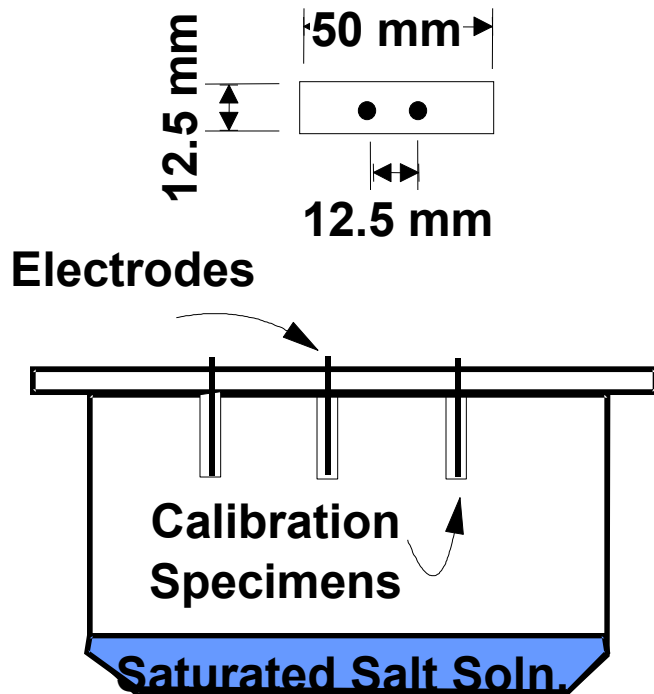


Drying



# Drying of a High w/c Systems

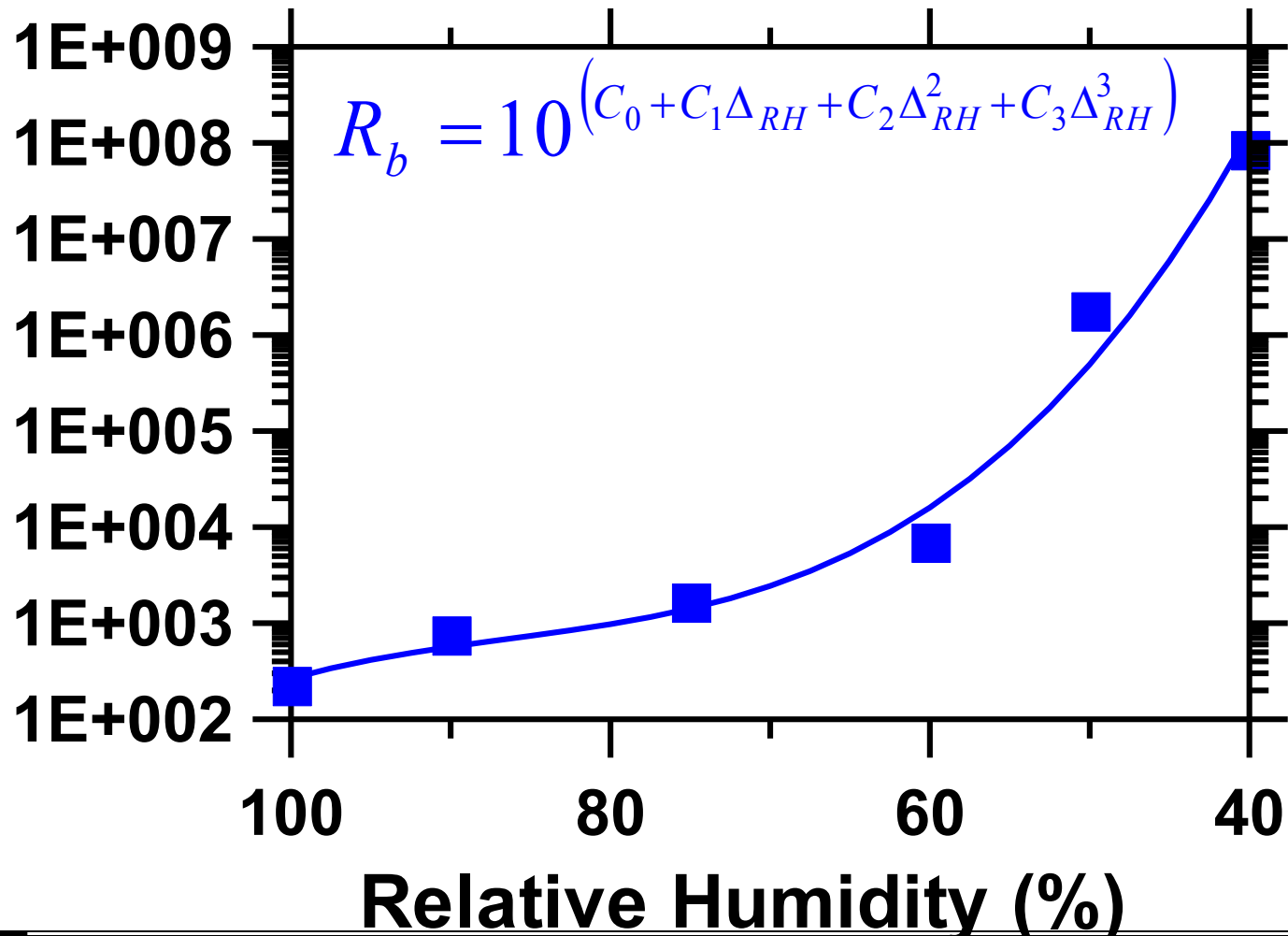
## Calibration Specimens





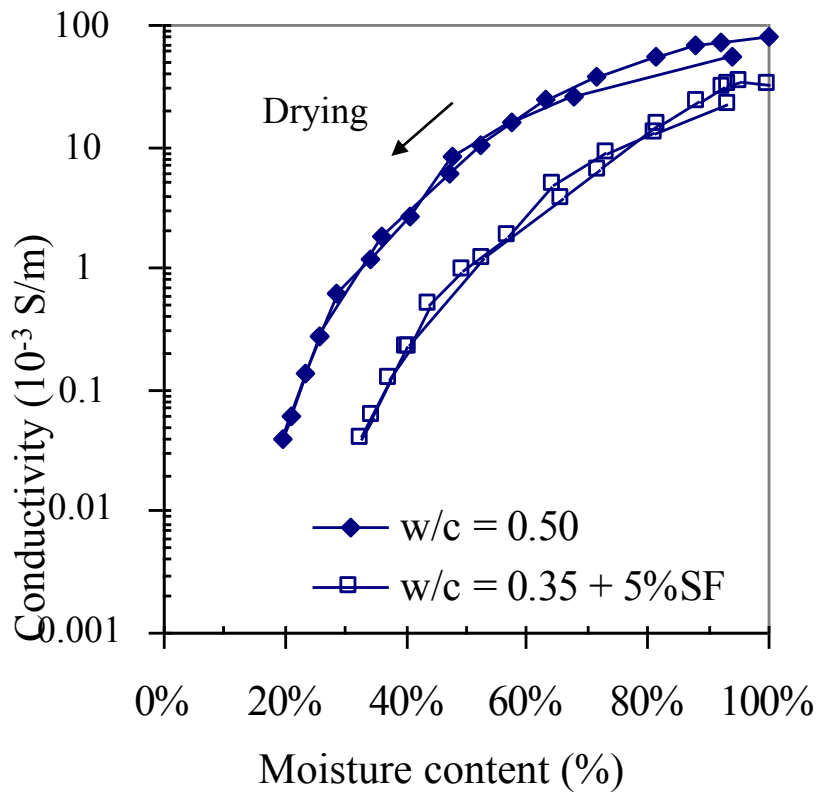
# Correlating Bulk Resistance with Humidity - 98 Days

Bulk Resistance (Ohms)

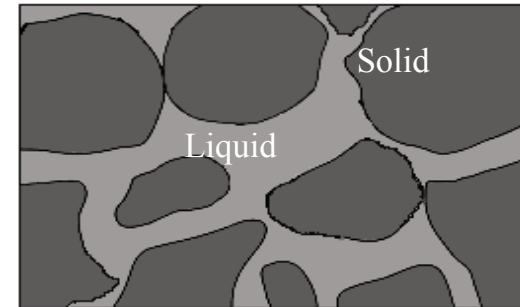




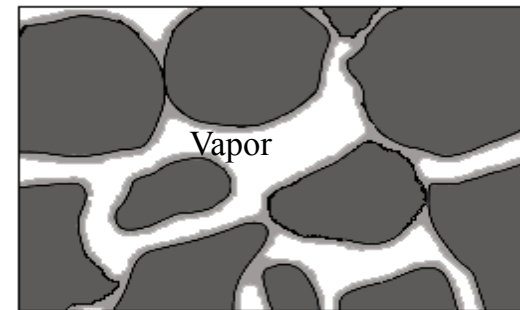
# What Parameters Affect Conductivity?



Saturated



Drying



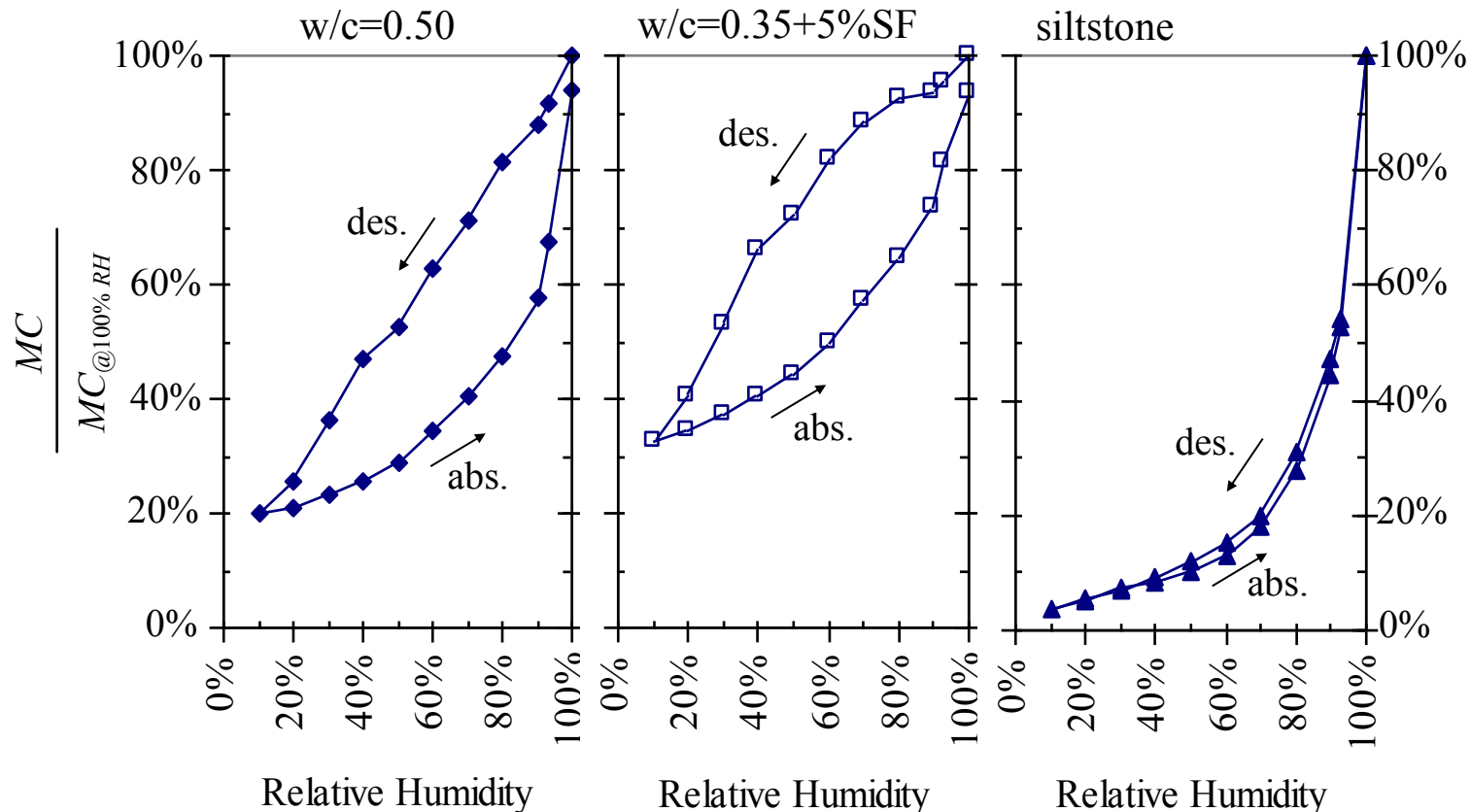
$$\sigma_t = \sigma_o \phi \beta$$

↓
↑
↓
↓

(Rajabipour and Weiss 2007)



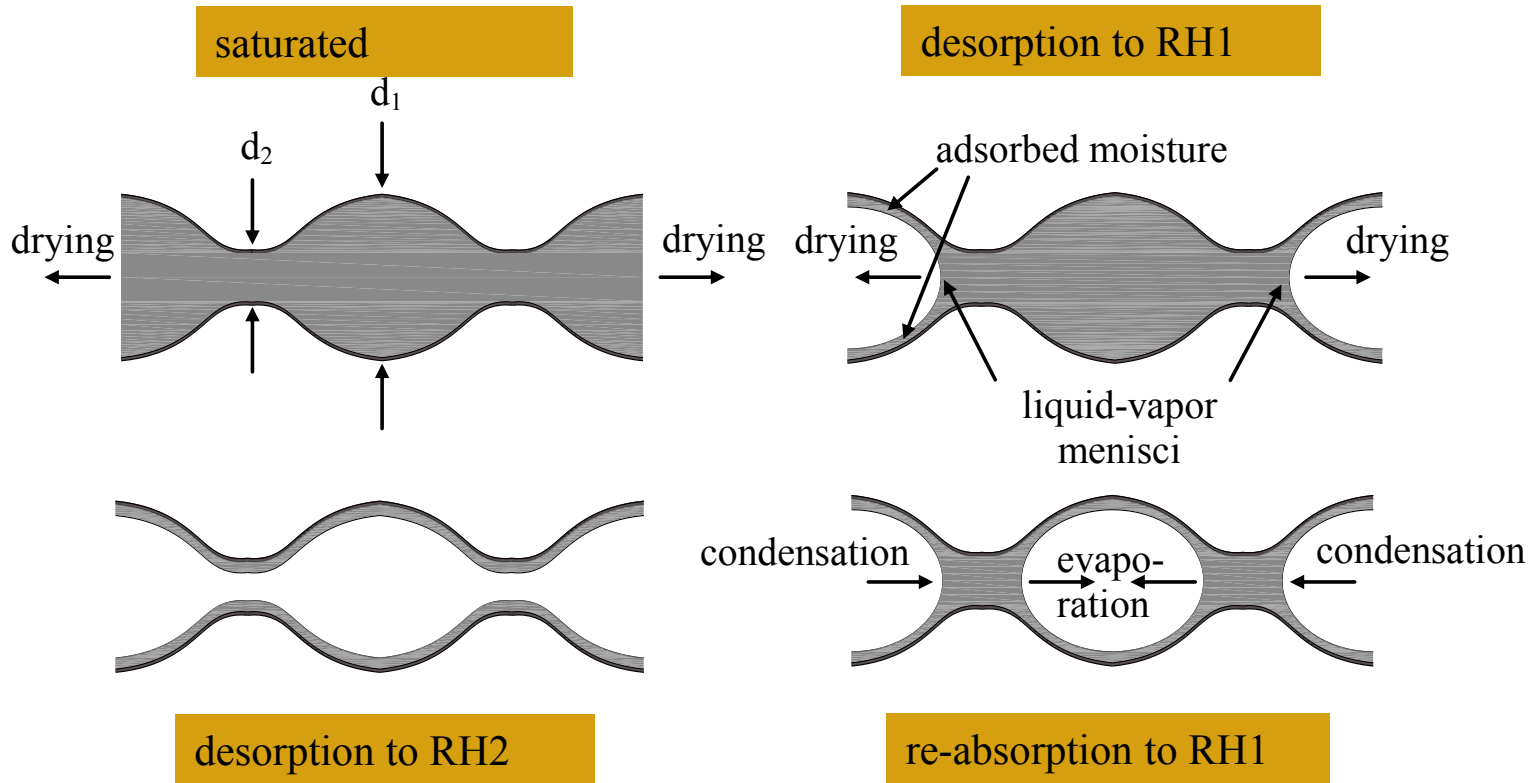
# Moisture Content Isotherms



Significant hysteresis in cement pastes



# Desorption-Absorption Hysteresis

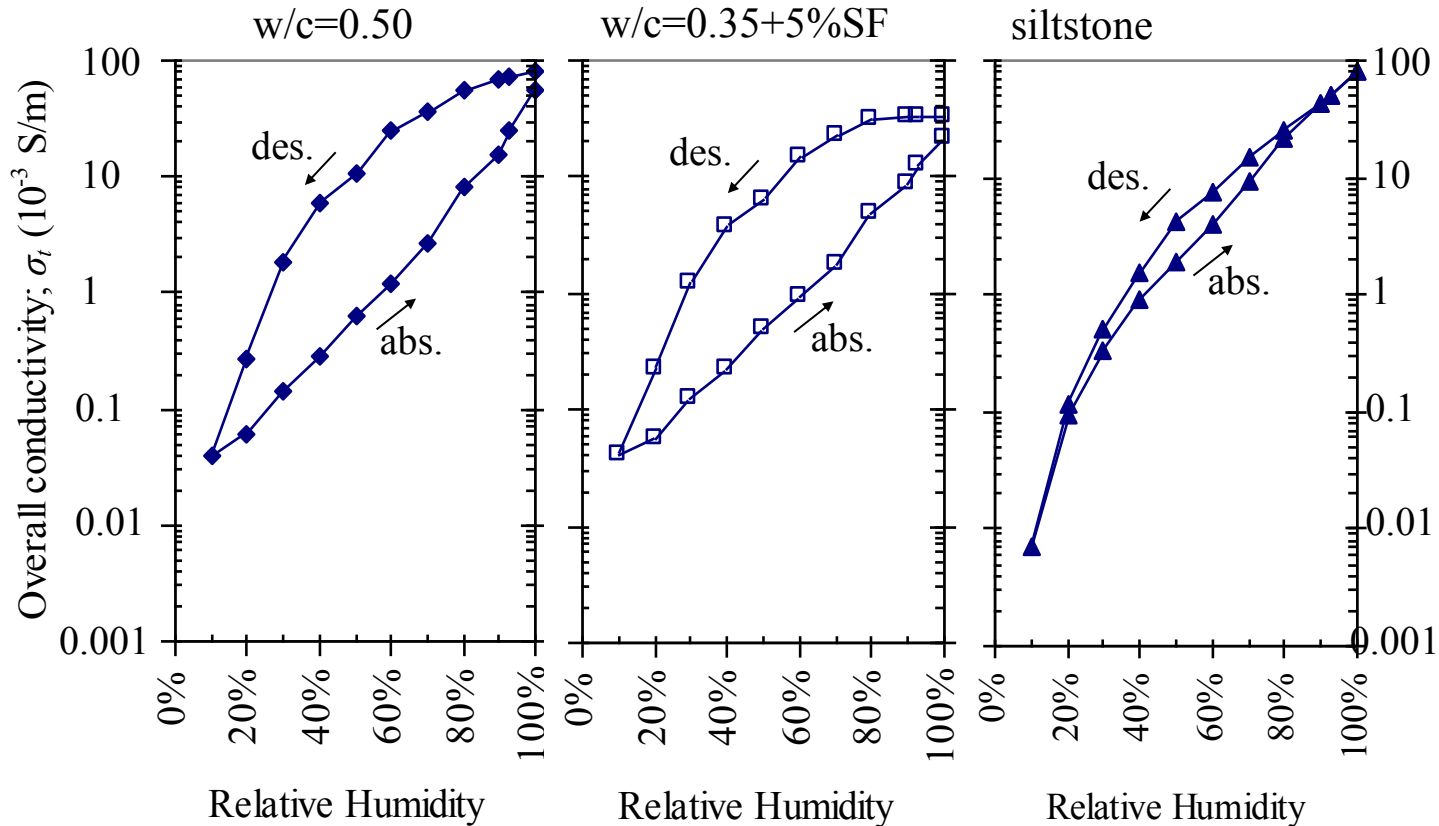


Feldman and Serada (1968):

- 1- Primary hysteresis at high to medium RH ( $>30\%$ ) due to pore constrictions
- 2- Secondary hysteresis at low RH ( $<30\%$ ) due to movement of interlayer water



# Electrical Conductivity Isotherms

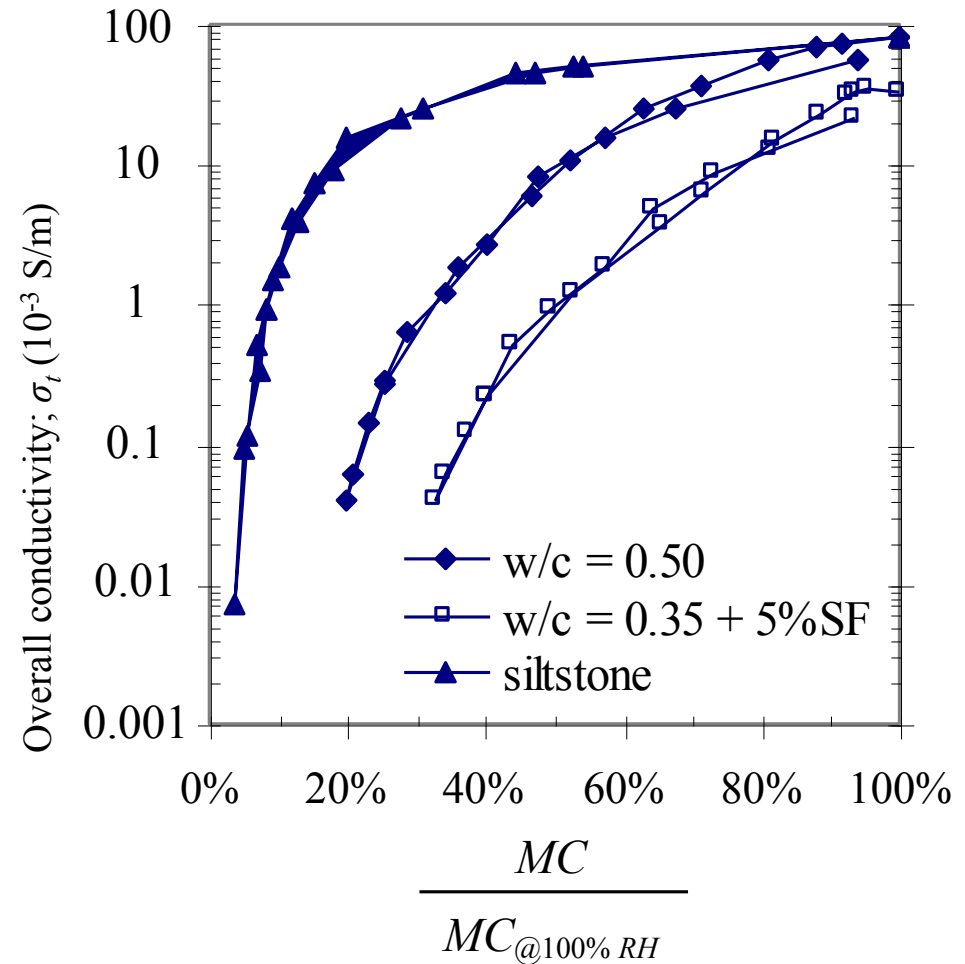


- Significant hysteresis for cement pastes
- $\sigma_t$  does not have a 1-to-1 correlation with RH (cement paste)
- estimation of RH based on  $\sigma_t$  can be erroneous (cement paste)



# Electrical Conductivity Isotherms

- $\sigma_t$  – MC: No hysteresis!!
- $\sigma_t$  – MC: 1-to-1 correlation
- MC the parameter governing

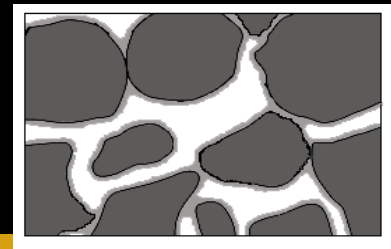




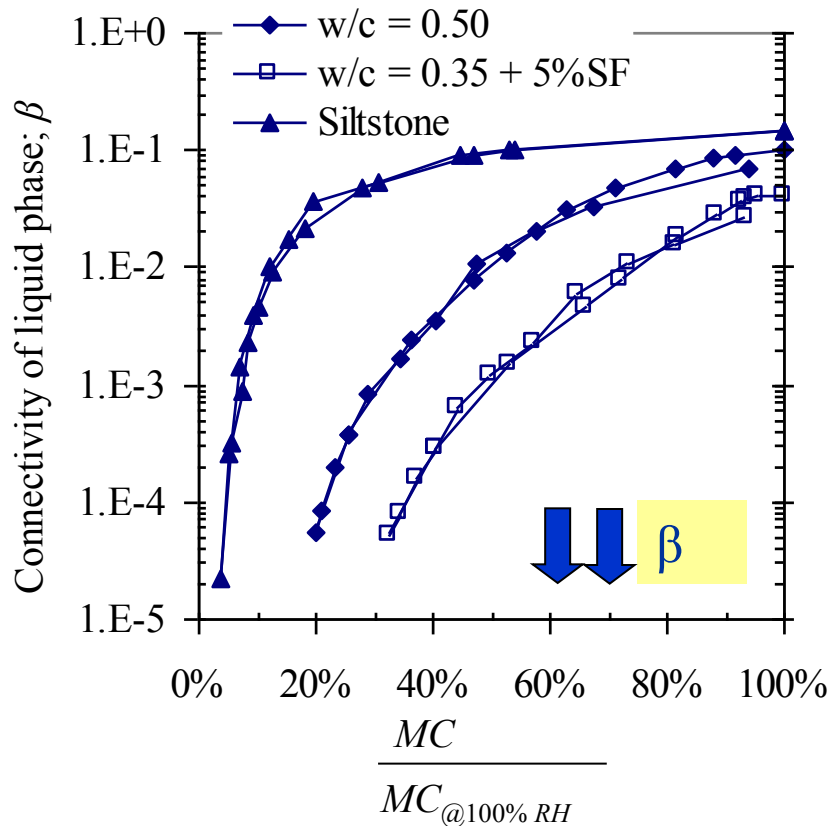


# Drying Cement Paste

## How $\sigma_t$ , $\sigma_o$ , $\phi$ , and $\beta$ change?



$$\sigma_t = \sigma_o \phi \beta$$



Moisture connectivity ( $\beta$ ) is the most influenced:

- Conduction paths become longer and more tortuous
- Conduction thru adsorbed moisture
- Adsorbed moisture breaks (>25%RH), disconnection of many conduction paths
- Depercolation of liquid phase (conduction partially thru solid)



# Alternative - Degree of Saturation

- Challenge:

- Difficult to deal with the equation as each term will change

$$\frac{\sigma_t}{\sigma_o} = a\phi^m$$

- Approach – describe the formation factor for a saturated system

$$\frac{\sigma_t}{\sigma_{o(s)}} = \frac{1}{F} f(S)$$

- The formation factor is the ratio of the resistivity with two solutions (system with water/system with brine)



# Degree of Saturation

- Challenge:
  - Difficult to deal with the equation as each term will change
  - Approach – describe the formation factor for a saturated system
  - Then apply a saturation function ( $S^n$ )

$$\frac{\sigma_t}{\sigma_o} = a\phi^m$$

$$\frac{\sigma_t}{\sigma_{o(S)}} = \frac{1}{F} f(S)$$

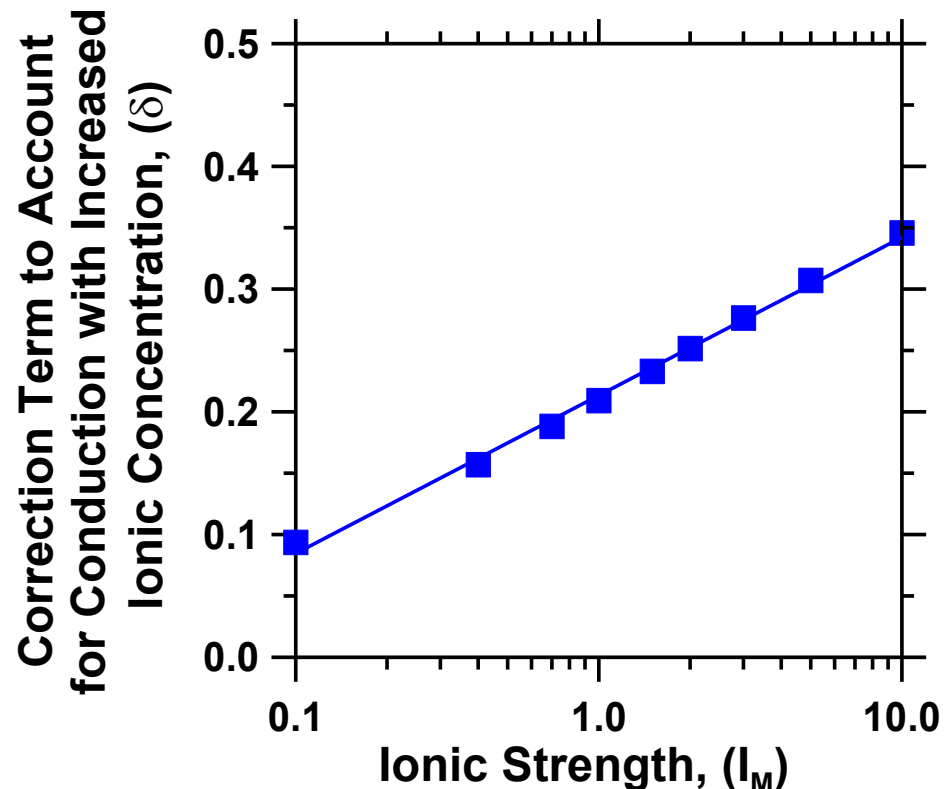
$$\sigma_t = \left( \frac{\sigma_{o(S=1)}}{S} \right) \left( \frac{1}{F} \right) f(S)$$



# Pore Solution Concentration

- Pore solution becomes more concentrated during drying

$$\frac{\sigma_o}{\sigma_{o(S=1)}} \cong \frac{1}{S} \left( \frac{1 + G\sqrt{I_M}}{1 + G\sqrt{\frac{1}{S}}\sqrt{I_M}} \right) = S^{\delta-1}$$

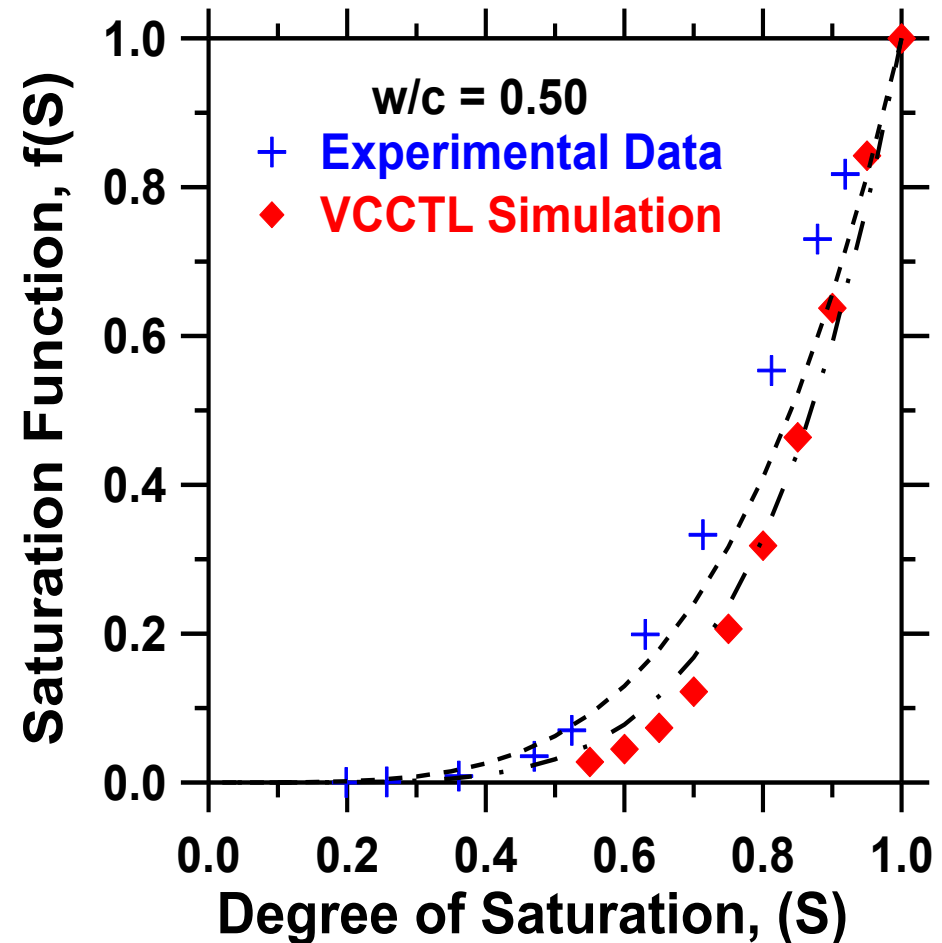




# Degree of Saturation

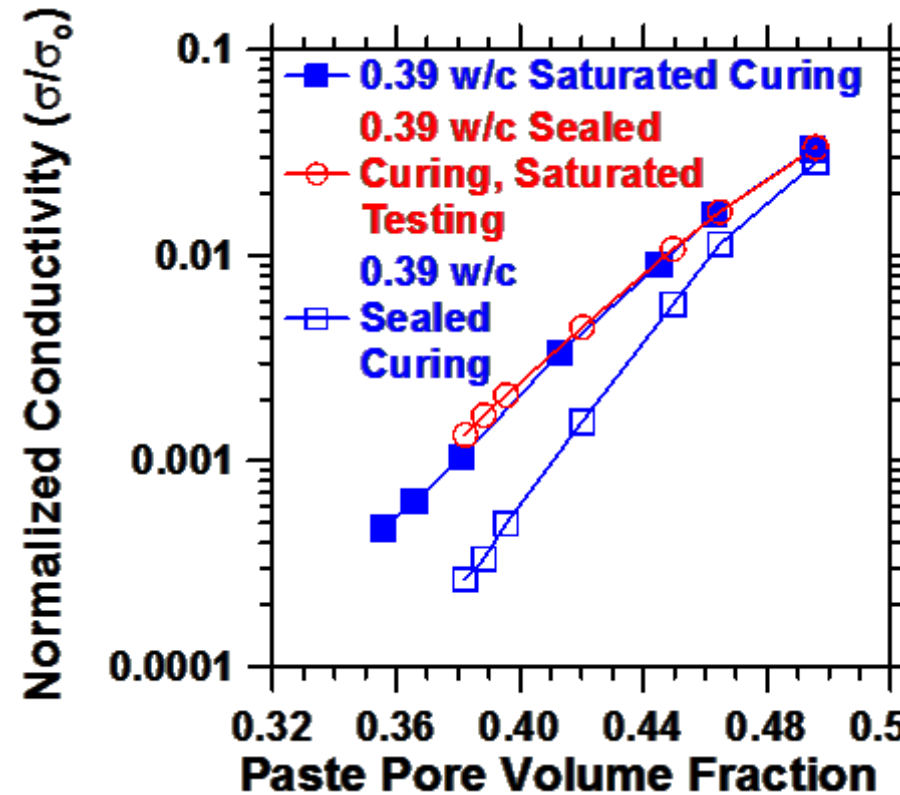
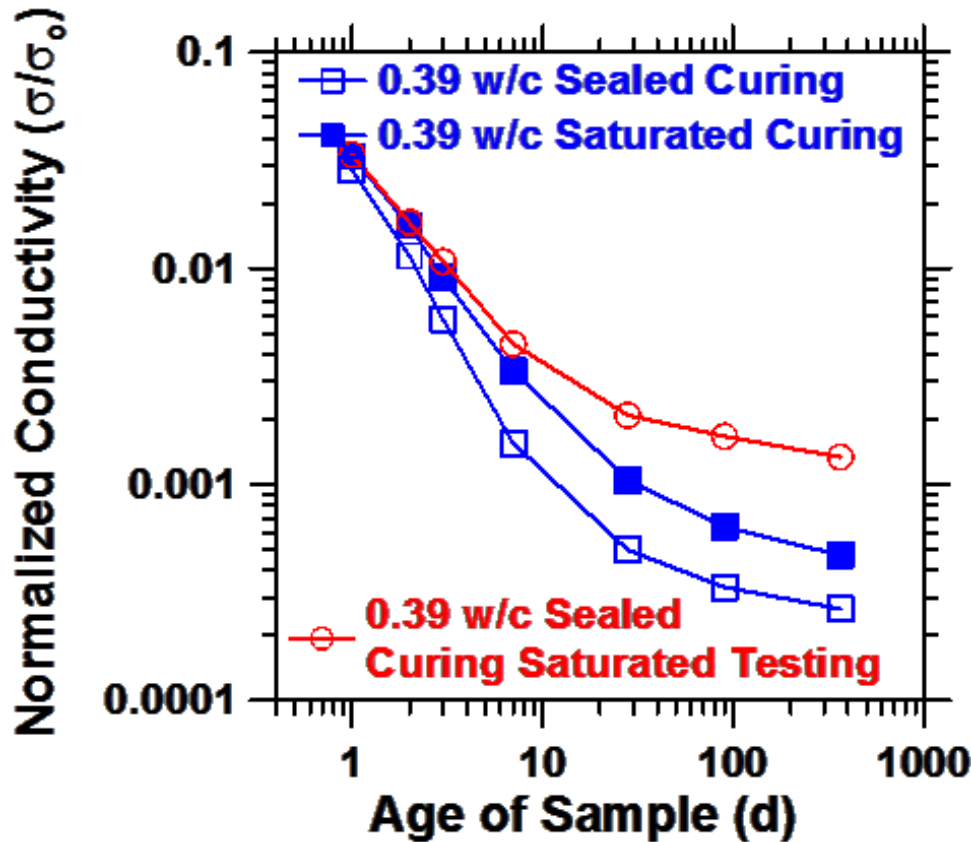
- Instead of correcting each term independently it may be possible to treat all the terms with a single function

$$\frac{\sigma_t}{\sigma_{o(S=1)}} = \frac{1}{F} S^{n-1+\delta}$$





# Curing/Saturation Conditions





# Saturation

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

Temperature

Leaching

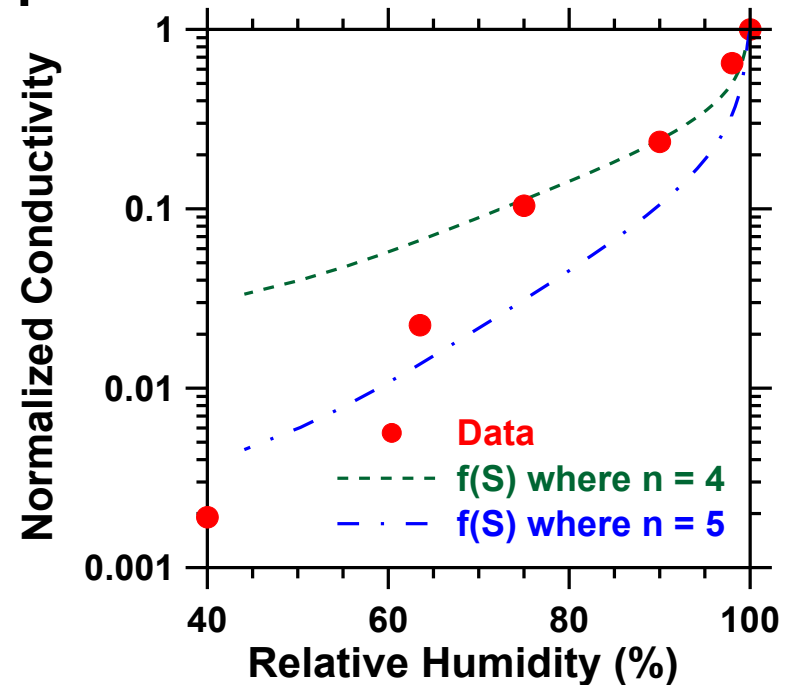
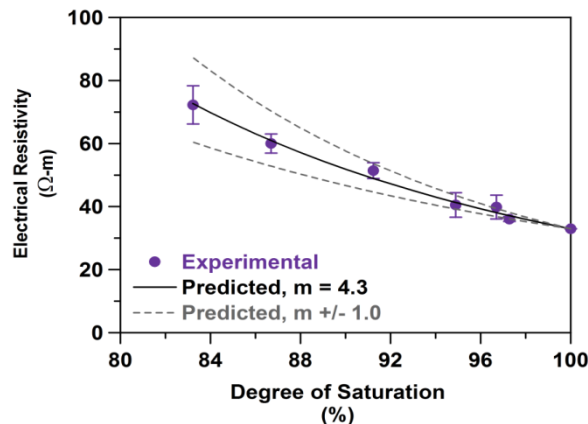
Acceleration

Field Use

- Weiss et al. (2012) approach accounted for loss of fluid, concentration of ions, and change in path, expression combines these

- $f(S) = S^m$

–  $m \approx 3 - 5$



Weiss et al. 2013

$$\rho = \rho_o^* \cdot F \cdot f(S) \cdot f(T_{Testing}) \cdot f(Leach) \text{ at } t_{equivalent}$$



# Incorporating Aspects of Curing

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

Temperature

Leaching

Acceleration

Field Use

- Spragg developed a program to investigate factors that could influence curing (not discussing temp or RH here that change DOH)

$$\rho = \rho_o^* \cdot F \cdot f(S) \cdot f(T_{Testing}) \cdot f(Leach)$$

- $\rho$  is the resistivity at an equivalent age  $t_{equivalent}$
- $\rho_o^*$ : pore solution resistivity at saturation
- $f(S)$  saturation function
- $f(T_{testing})$  testing temperature correction
- $f(Leach)$  leaching function

Spragg et al. 2013





# Maturity and Electrical Conductivity

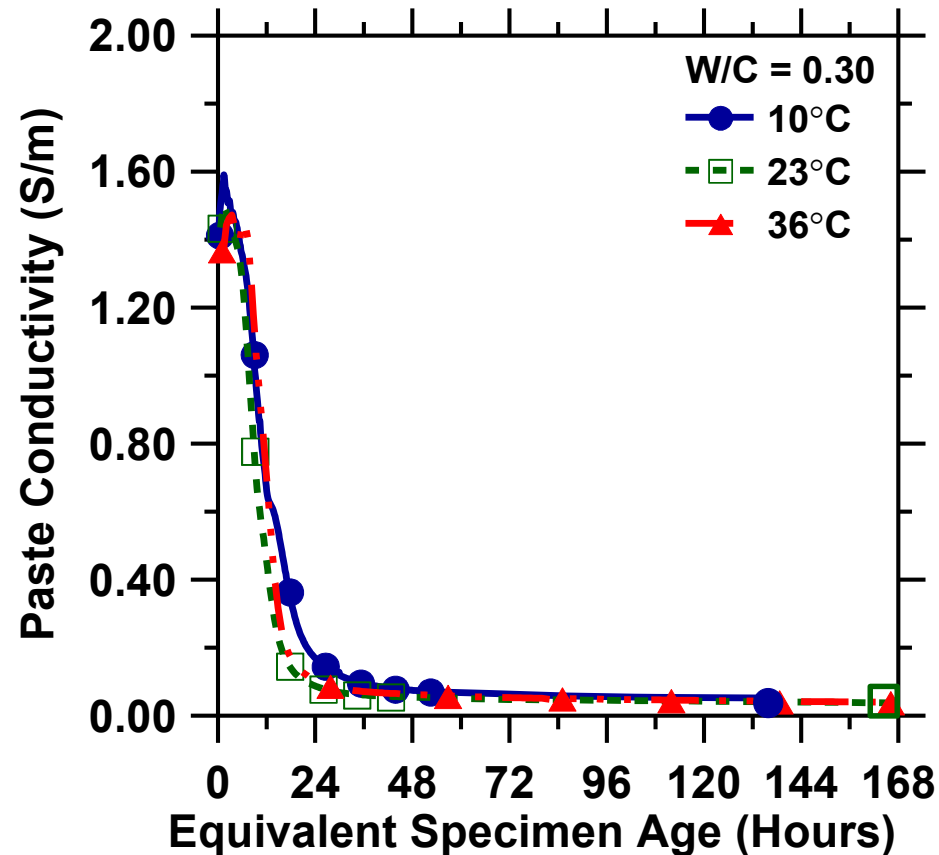
- Conductivity is a function of Maturity (hydration) and Temperature (conductivity)

$$\sigma(t) = f(M) \cdot f(T)$$

$$f(M) = \int_0^t \exp\left[\frac{E_{aR}}{R} \cdot \left(\frac{1}{T} - \frac{1}{T_{REF}}\right)\right] \cdot dt$$

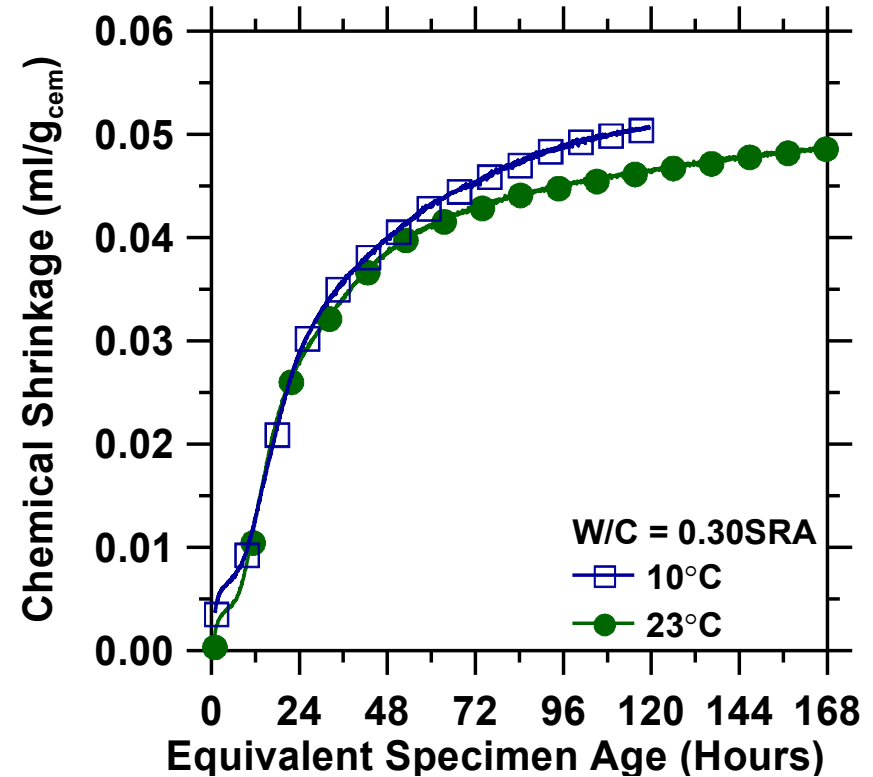
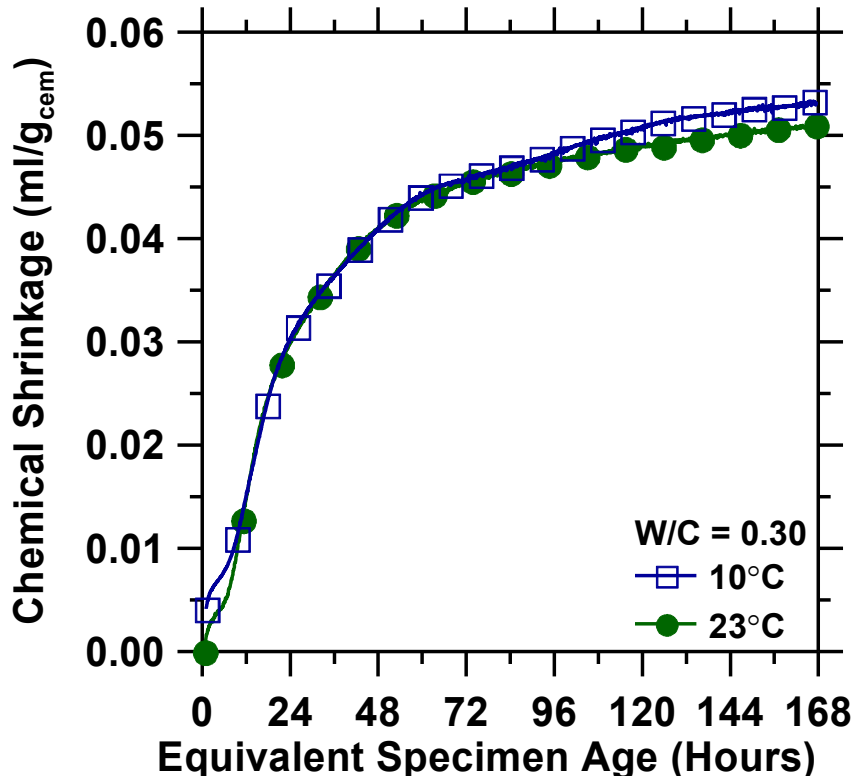
$$E_{aR} = 39.50 \text{ KJ/mole}$$

$$f(T) = \frac{\sigma(T)}{\exp\left(-\frac{E_{aC}}{R} \cdot \left(\frac{1}{T} - \frac{1}{T_{REF.}}\right)\right)}$$





# Applicability of a Maturity Transformation to Cement Hydration



- Concept is applicable
- EAR = 37.5 KJ/mol
- Minor variations related

$$t_e = \int_0^t \exp \left[ \frac{E_{aR}}{R} \cdot \left( \frac{1}{T} - \frac{1}{T_{REF}} \right) \right] \cdot dt$$



# Testing Temperature

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

Temperature

Leaching

Acceleration

Field Use

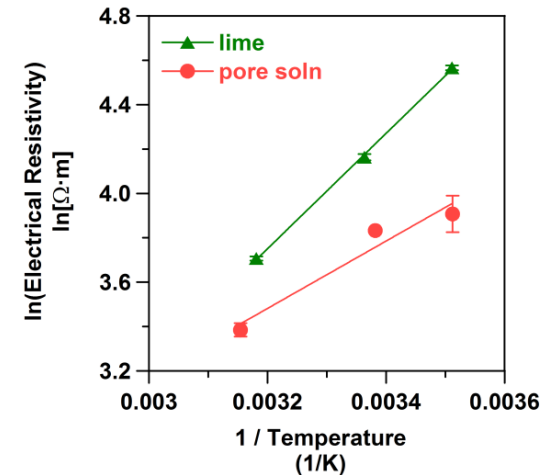
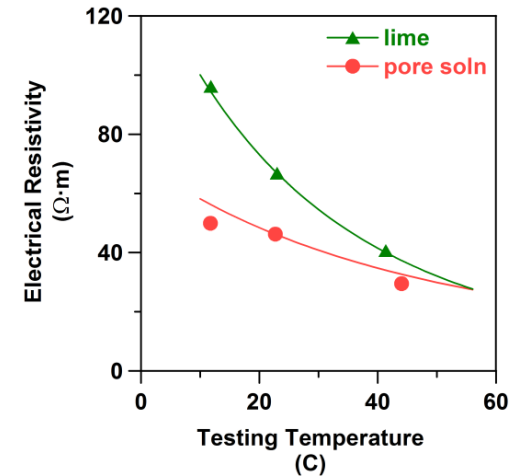
- Activation Energy of Conduction (test temp)

Rajabipour et al. 2007, Sant et al. 2007

$$\frac{\rho_{T_{ref}}}{\rho} = \exp \left[ \frac{E_{a-con}}{R} \left( \frac{1}{T} - \frac{1}{T_o} \right) \right]$$

- In the past we noticed differences between
- Varied the solutions
  - Pore Solution: 9-12 kJ/mol
  - Bulk Sample: 20-25 kJ/mol

$$\rho = \rho_o^* \cdot F \cdot f(S) \cdot f(T_{Testing}) \cdot f(Leach) \text{ at } t_{equivalent}$$

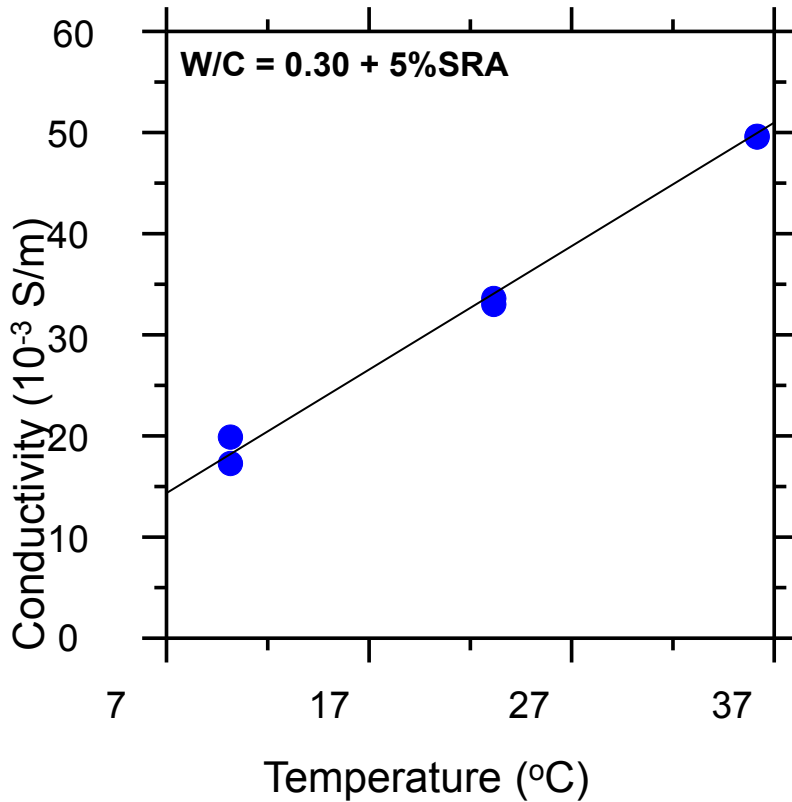


Spragg et al. 2013

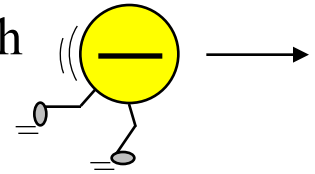


# Arrhenius Law

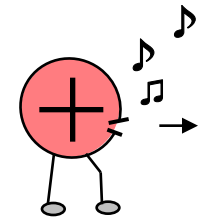
w/c	E <sub>ac</sub> (KJ/mole)
0.36	9.39
0.42	10.19
0.45	10.06
0.50	9.69
<b>STD DEV</b>	0.365



- High Temperature: High mobility, fast ions High conductivity



- Low Temperature: Low mobility, slow ions Low conductivity



$$\sigma(T) = Ae^{\left(\frac{-E_a}{RT}\right)}$$

- Higher temperature → higher conductivity

(Rajabipour 2006, Sant et al. 2008)



# Maturity and Electrical Conductivity

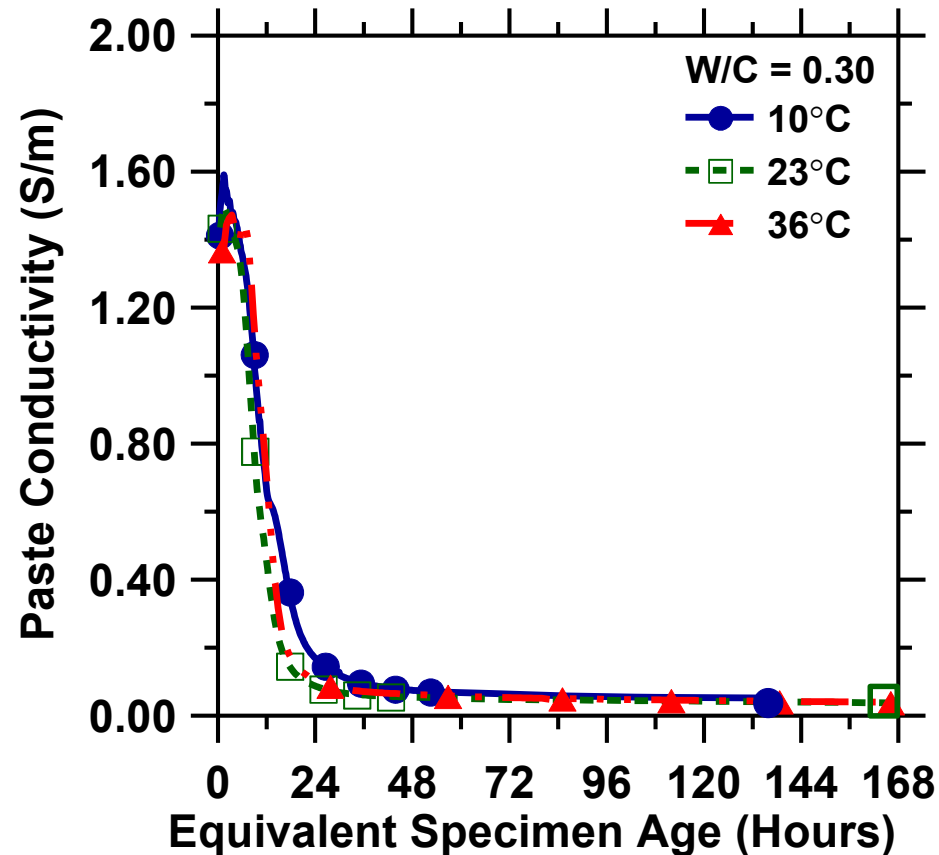
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$$E_{aR} = 39.50 \text{ KJ/mole}$$

$$f(T) = \frac{\sigma(T)}{\exp\left(-\frac{E_{aC}}{R} \cdot \left(\frac{1}{T} - \frac{1}{T_{REF.}}\right)\right)}$$





# Incorporating Aspects of Curing

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

Temperature

Leaching

Acceleration

Field Use

- Spragg developed a program to investigate factors that could influence curing (not discussing temp or RH here that change DOH)

$$\rho = \rho_o^* \cdot F \cdot f(S) \cdot f(T_{Testing}) \cdot f(Leach)$$

- $\rho$  is the resistivity at an equivalent age  $t_{equivalent}$
- $\rho_o^*$ : pore solution resistivity at saturation
- $f(S)$  saturation function
- $f(T_{testing})$  testing temperature correction
- $f(Leach)$  leaching function

Spragg et al. 2013



# Leaching During Storage

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

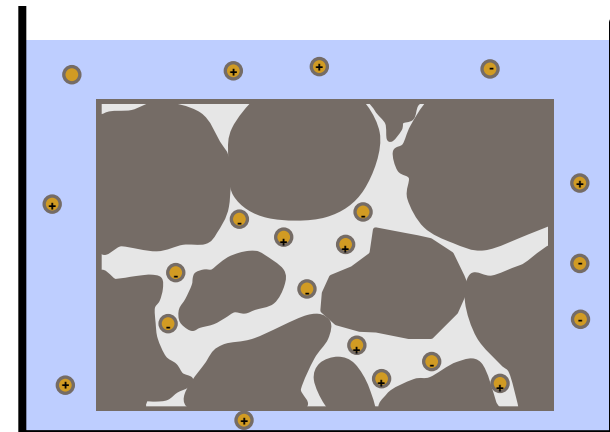
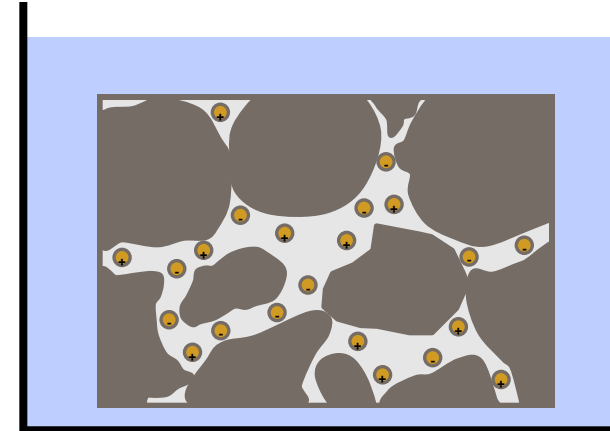
Temperature

Leaching

Acceleration

Field Use

- Many people think of CH leaching
- However we are worried about alkali leaching
- Cement pore solution
  - $\text{OH}^-$ ,  $\text{K}^+$ ,  $\text{Na}^+$
  - $\rho \approx 40\text{--}100$  m ohm·m
- Standard Solution
  - $\text{CaOH}_2$  (CH)
  - $\rho \approx 1000$  milli ohm·m
- Measured storage solution



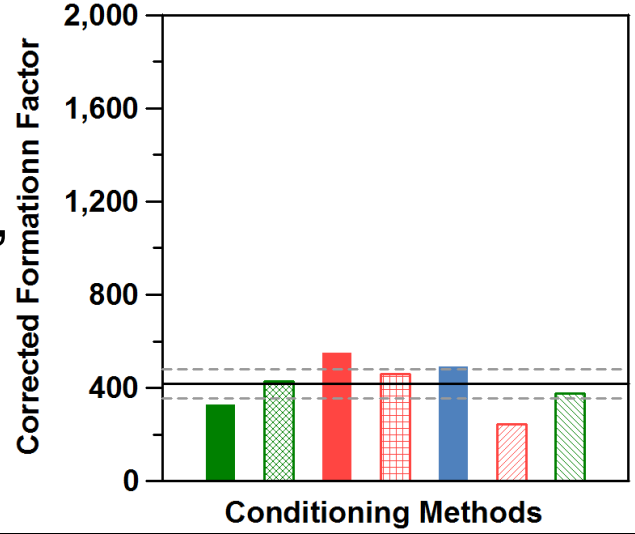
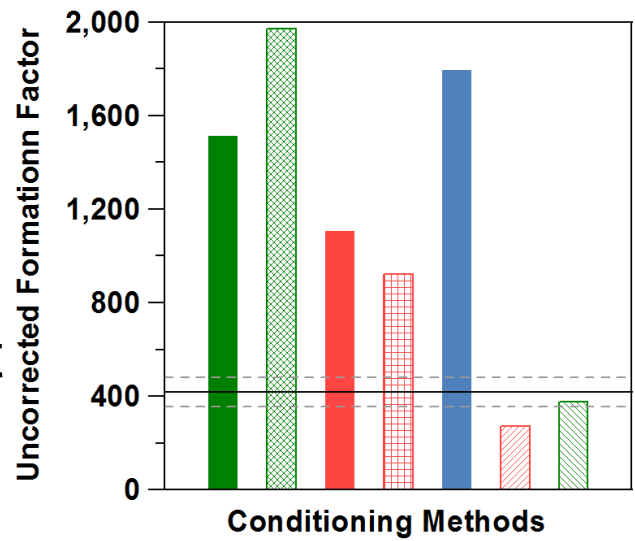
Spragg et al. 2013



# Importance of Accounting for Several Factors

$\sigma, \rho$   
 Geometry  
 3 Factors  
 Pore soln  
 Porosity  
 Tortuosity  
 Variability  
 Saturation  
 Temperature  
 Leaching  
 Acceleration  
 Field Use

- Formation Factor – 420
- Top figure shows direct measurement
- Bottom has corrections applied for temperature, ionic strength, saturation, and leaching



Lime Water, 23C  
 Lime Water, 45C  
 Pore Solution, 23C  
 Pore Solution, 45C  
 Sealed  
 Vac Sat: Pore Solution  
 Vac Sat: Lime Water  
 Ionic Diffusion Test  
 +/- 3 st dev IDC

Lime Water, 23C  
 Lime Water, 45C  
 Pore Solution, 23C  
 Pore Solution, 45C  
 Sealed  
 Vac Sat: Pore Solution  
 Vac Sat: Lime Water  
 Ionic Diffusion Test  
 +/- 3 st dev IDC

Spragg et al. 2013





# Accelerating Curing Time

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

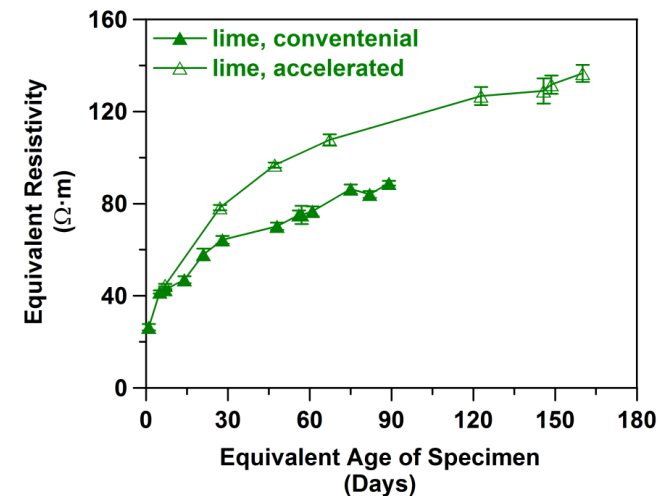
Temperature

Leaching

Acceleration

Field Use

- Many materials we test take a long time to show benefits (91 d)
- We frequently want to speed this time up
- VTRC/NRMCA method
- Lime water 7d, 23C followed by 21d, 38C
- T equivalent 56d
- Application on the right shows difference ~25%



Bu et al. 2014



# Accelerated Curing Effects

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

Temperature

Leaching

Acceleration

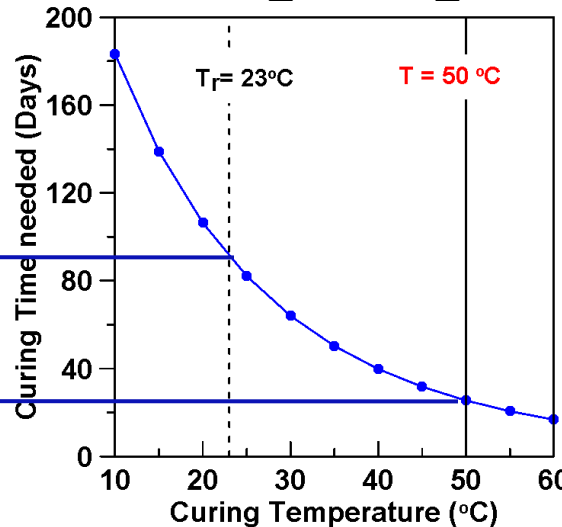
Field Use

Transport testing and service life prediction usually performed on specimens of later age (91 days).

$$t_e = e^{-\frac{E_a}{R} \left( \frac{1}{T} - \frac{1}{T_r} \right)} t$$

Same maturity (DOH) could be achieved with shorter time using a higher curing temperature.

91 days  
23 days  
days



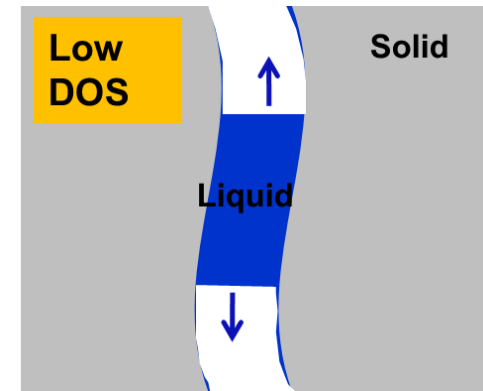
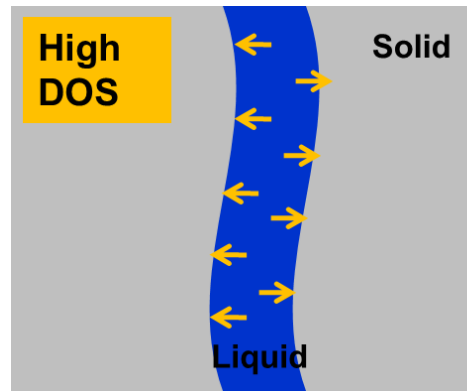
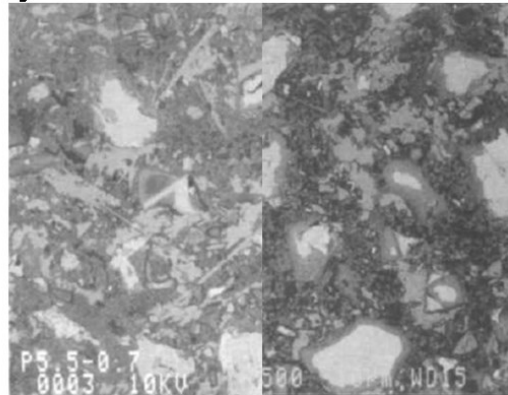
$E_a = 37$   
kJ/mol

Bu et al. 2014



# Role of Fluid Expansion

Kjellson et al. 1990



- Examined normal and accelerated curing with samples at different temperatures that were sealed/saturated

	Porosity (%)	$D_{Cl^-}$ ( $10^{-11} \text{ m}^2/\text{s}$ )
<b>NA-Wet</b>	<b>16.4</b>	<b>3.66</b>
<b>AA- Sealed</b>	<b>16.3</b>	<b>3.71</b>
<b>AA- Wet</b>	<b>17.5</b>	<b>4.81</b>

**Saturated Samples 24%**

Bu et al. 2014

- $\sigma, \rho$
- Geometry
- 3 Factors
- Pore soln
- Porosity
- Tortuosity
- Variability
- Saturation
- Temperature
- Leaching
- Acceleration
- Field Use



# Applications – Acceptance Phase

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

Temperature

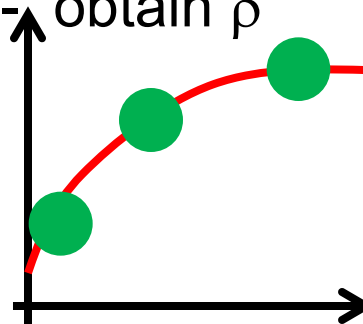
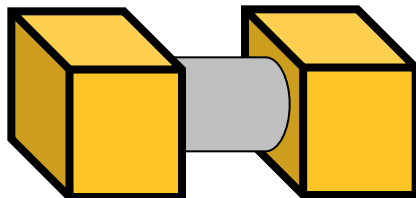
Leaching

Acceleration

Field Use

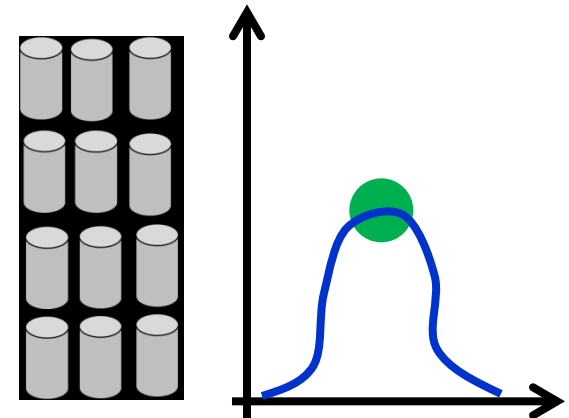
## Mixture Acceptance

- Before construction to “qualify mixture”
- Time to corrosion
  - Absolute value of D
- Development of master curve data
  - strength v time
  - resistivity v time
- Specify F ---- obtain  $\rho$



## Quality Control

- Measurements during construction
- Test with good repeatability
- Easy tests allow for large sample size, statistical information as well





# Summary and Recommendations

$\sigma, \rho$

Geometry

3 Factors

Pore soln

Porosity

Tortuosity

Variability

Saturation

Temperature

Leaching

Acceleration

Field Use

- Electrical properties
  - resistivity is a material property (geometry)
  - F is a material property (defined saturated)
  - test temperature important
  - degree of saturation
  - ionic leaching
  - curing can have major impact on variability
- Accelerated Curing
  - Maturity Method Can Be Applied
  - Accelerated Aging Causes Differences – Suggest Sealed Samples (low Pressure)